



## Complete transverse 4D beam characterization for ions at energies of a few MeV/u

M. Maier, X.N. Du, P. Gerhard, L. Groening, S. Mickat, H. Vormann, and C. Xiao  
*GSI Helmholtzzentrum für Schwerionenforschung GmbH, D-64291 Darmstadt, Germany*

- **Introduction**
  - the transverse beam matrix and beam emittance
  - slit-grid Emittance scanners
- **Motivation**
  - decrease of projected emittance
  - flat beam creation by emittance transfer
- **Experimental setups and results**
  - EMTEX and the skew method
  - ROSE
    - working principle
    - technical solutions
    - commissioning
- **Summary & outlook**

# Introduction

## equations for transverse emittance



The four-dimensional symmetric beam matrix C:

For a decoupled beam the off-diagonal matrix elements (red) are zero.

$$C = \begin{bmatrix} \langle xx \rangle & \langle xx' \rangle & \langle xy \rangle & \langle xy' \rangle \\ \langle x'x \rangle & \langle x'x' \rangle & \langle x'y \rangle & \langle x'y' \rangle \\ \langle yx \rangle & \langle yx' \rangle & \langle yy \rangle & \langle yy' \rangle \\ \langle y'x \rangle & \langle y'x' \rangle & \langle y'y \rangle & \langle y'y' \rangle \end{bmatrix}$$

$$\text{with } \varepsilon_x = \sqrt{\det \sigma_x}$$

$$\sigma = \begin{pmatrix} \sigma_{11} & \sigma_{12} \\ \sigma_{12} & \sigma_{22} \end{pmatrix} = \varepsilon \cdot \begin{pmatrix} \beta & -\alpha \\ -\alpha & \gamma \end{pmatrix}$$

$$\varepsilon_x = \sqrt{\det \sigma} = \sqrt{\sigma_{11}\sigma_{22} - \sigma_{12}^2}$$

$\alpha$ ,  $\beta$ ,  $\gamma$  are the Twiss parameters and  $\varepsilon_x$  is the horizontal rms-emittance



## if the beam is not decoupled?

The four-dimensional rms emittance:  $\varepsilon_{4d} = \varepsilon_1 \varepsilon_2 = \sqrt{\det C}$

Diagonalization of the beam matrix yields the Eigen-emittances  $\varepsilon_1$  and  $\varepsilon_2$  which are:

$$\varepsilon_1 = \frac{1}{2} \sqrt{-\text{tr}[(CJ)^2] + \sqrt{\text{tr}^2[(CJ)^2] - 16\det(C)}}$$

$$\varepsilon_2 = \frac{1}{2} \sqrt{-\text{tr}[(CJ)^2] - \sqrt{\text{tr}^2[(CJ)^2] - 16\det(C)}}$$

A coupling parameter  $t$  is introduced to quantify the inter-plane coupling and defined as:

$$t = \frac{\varepsilon_x \varepsilon_y}{\varepsilon_1 \varepsilon_2} - 1 \geq 0,$$

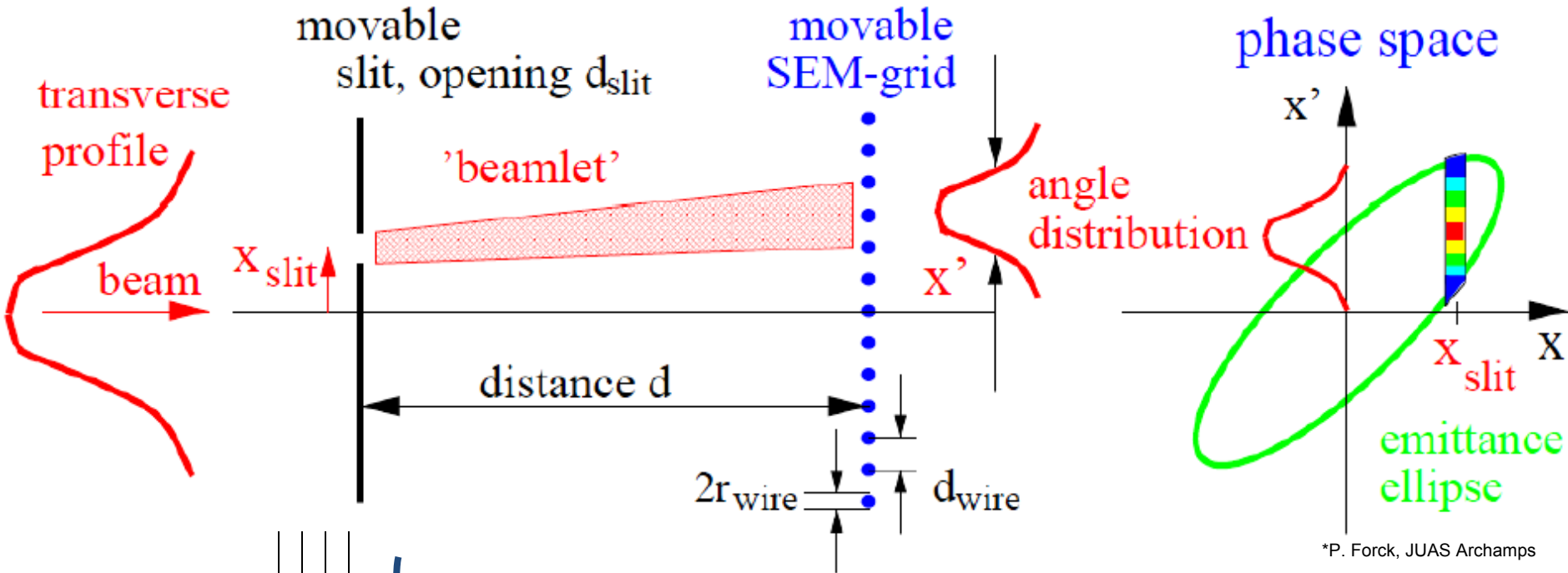
In other words  $\varepsilon_1$  and  $\varepsilon_2$  are the rms-emittances of a fully decoupled beam.

**or in simple words:** uncoupled beams are an idealization to simplify the beam dynamics and are a best case scenario. If the beam is correlated the projected emittance is larger than necessary and could be decreased!

# Emittance measurements: Slit-grid (concept)

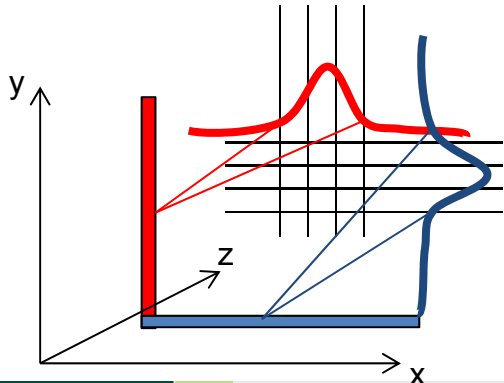
## Hardware

## Analysis



\*P. Forck, JUAS Archamps

**A slit-grid emittance measurement in one plane is always integrating over the other plane**

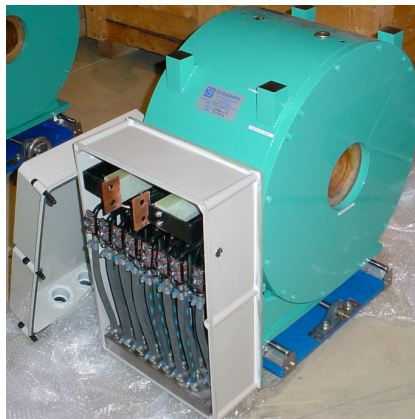


# Motivation: Envelopes along Solenoid Channel

initial beam:

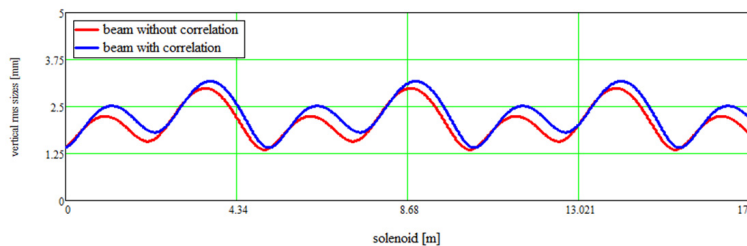
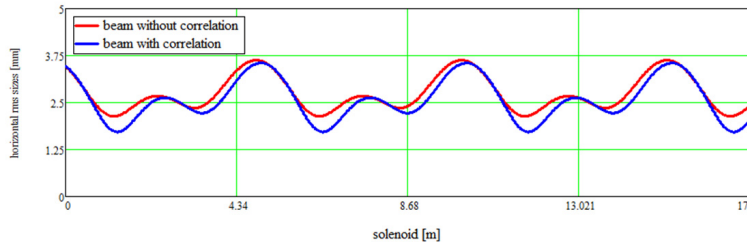
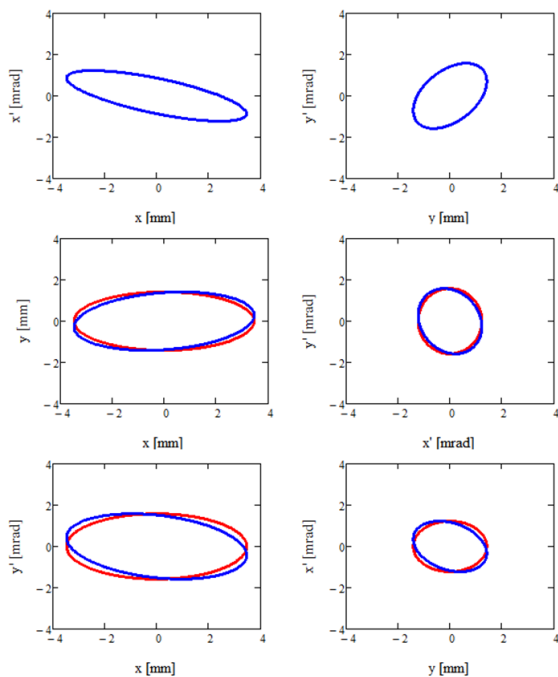
$$C_1 = \begin{bmatrix} 12.00 & -3.00 & 0.00 & 0.00 \\ -3.00 & 1.50 & 0.00 & 0.00 \\ 0.00 & 0.00 & 2.00 & 1.00 \\ 0.00 & 0.00 & 1.00 & 2.50 \end{bmatrix} \text{ uncorrelated}$$

$$C_2 = \begin{bmatrix} 12.00 & -3.00 & 1 & -1.5 \\ -3.00 & 1.50 & -0.5 & -0.35 \\ 1.00 & -0.50 & 2.00 & 1.00 \\ -1.50 & -0.35 & 1.00 & 2.50 \end{bmatrix} \text{ correlated}$$

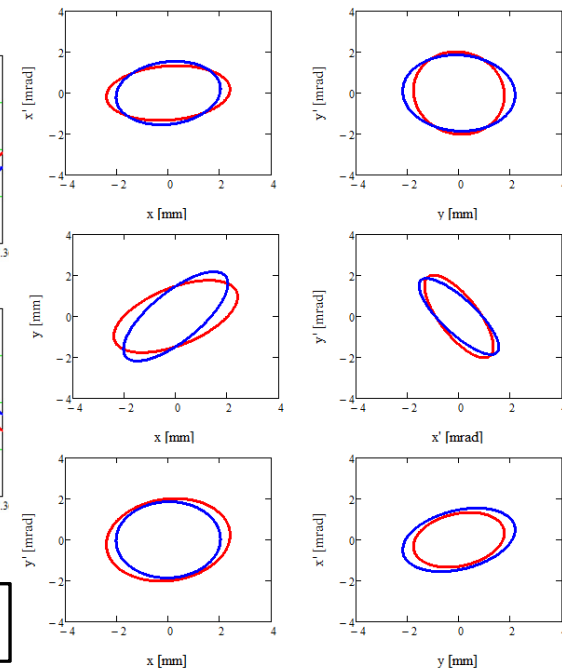


$$M_{sol} = \begin{bmatrix} C^2 & \frac{SC}{K} & SC & \frac{S^2}{K} \\ -KSC & C^2 & -KS^2 & CS \\ -SC & -\frac{S^2}{K} & C^2 & \frac{SC}{K} \\ KS^2 & -SC & -KSC & C^2 \end{bmatrix}$$

final beam:



**red and blue envelopes differ**



# Motivation: EMTEX

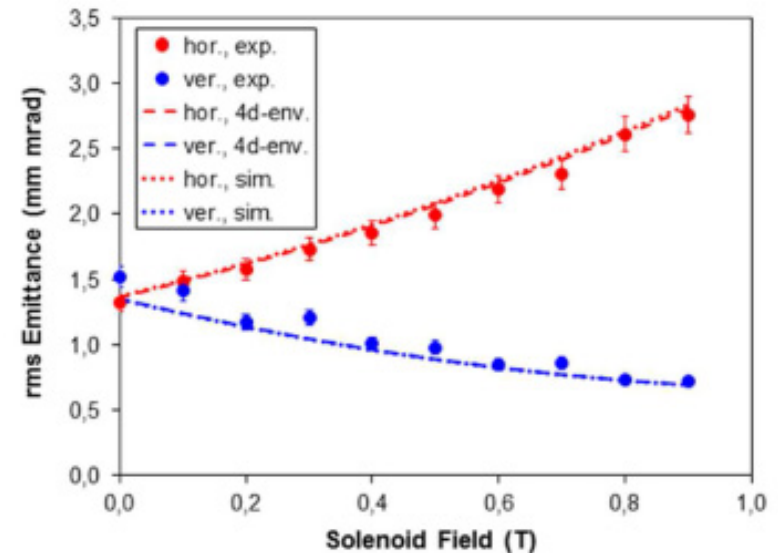
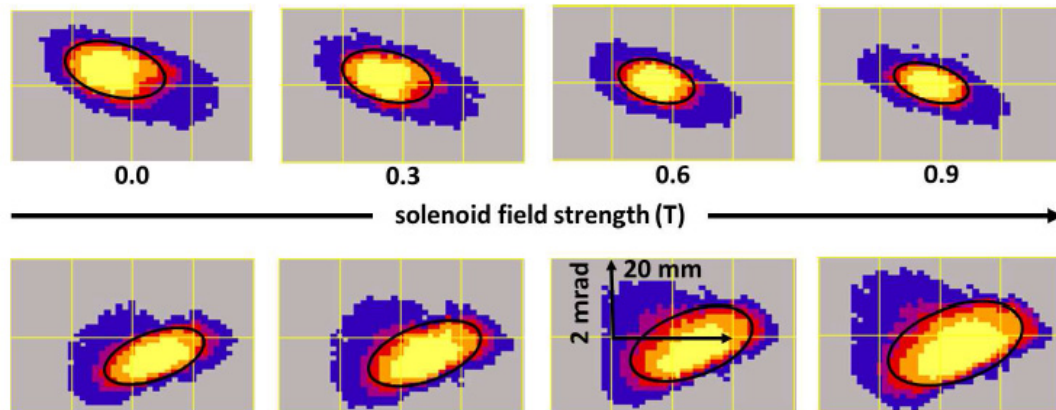
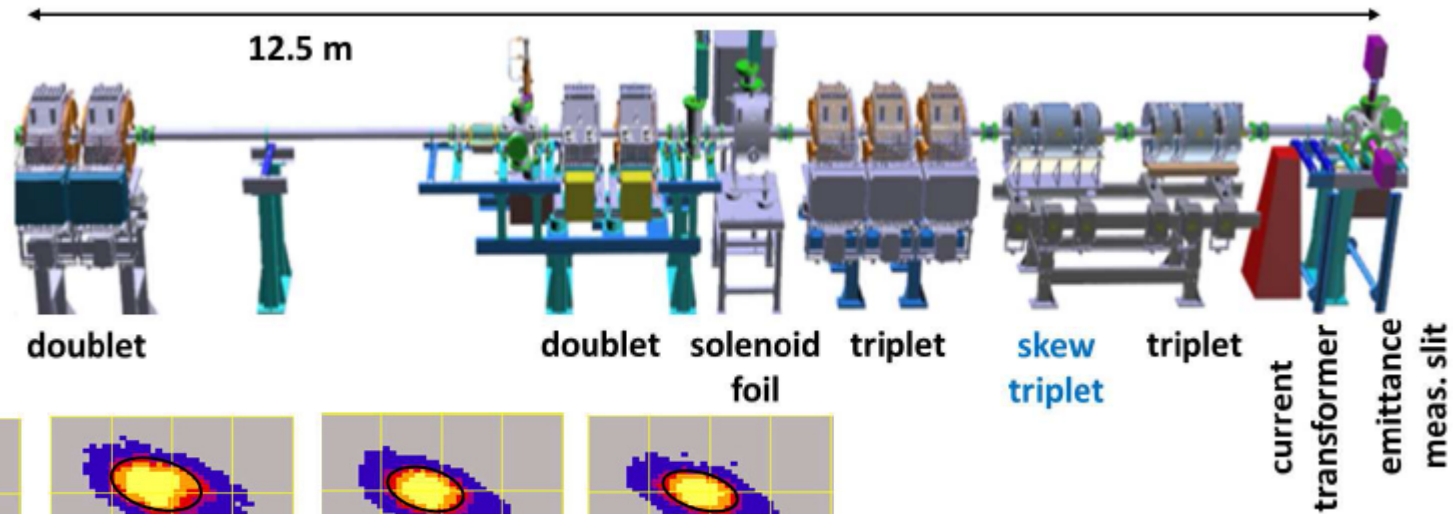


FIG. 4. (color online) Vertical (upper) and horizontal (lower) phase space distributions measured at the exit of the EMTEX beam line as functions of the solenoid field strength. All other settings were kept constant. Black ellipses indicate the  $4\times$  rms ellipses.

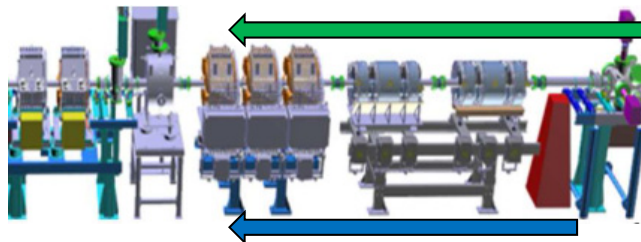
Physical Review Letters, 113, (2014) 264802

# Experimental results

## skew method

Emittance measurements on a 1.7mA  $^{238}\text{U}^{28+}$  beam behind the skew quadrupole of EMTEX have been used to measure the 4D emittance. The emittance measurement without using the skew quadrupole **assuming an uncorrelated beam** at the entrance of EMTEX results in the second-moment beam matrix:

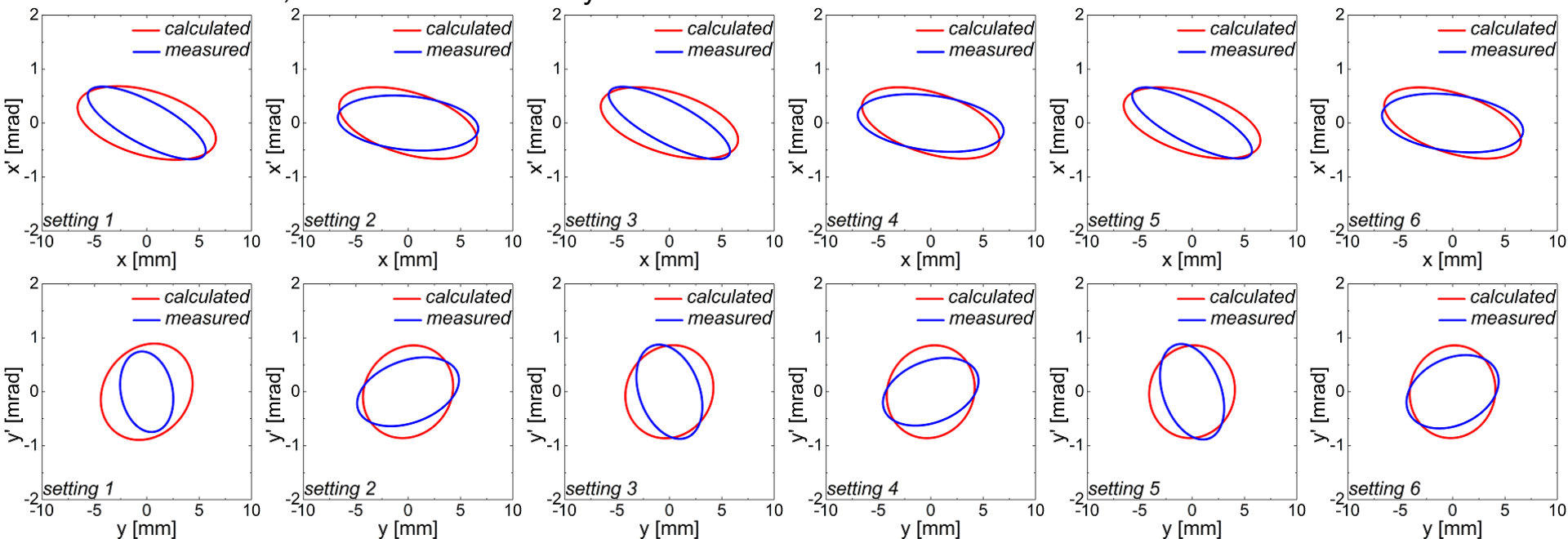
$$C_0 = \begin{pmatrix} 12.79 & 1.89 & 0 & 0 \\ 1.89 & 0.62 & 0 & 0 \\ 0 & 0 & 32.18 & 3.49 \\ 0 & 0 & 3.49 & 0.46 \end{pmatrix}$$



$$\begin{aligned} \alpha_x &= -0.902, \alpha_y = -2.160 \\ \beta_x &= 6.11, \beta_y = 19.89 \text{ m/rad} \\ \varepsilon_x &= 2.1, \varepsilon_y = 1.6 \text{ mm*mrad} \end{aligned}$$

setting 1-6

Repeating the measurements for turned on skews and comparing them to the simulations, using the above uncorrelated matrix, does not fit sufficiently well! Thus it is concluded the initial beam inherits correlations.



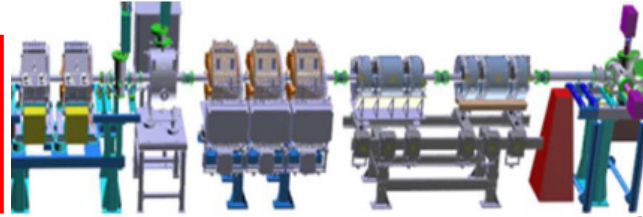


# Experimental results

## skew method

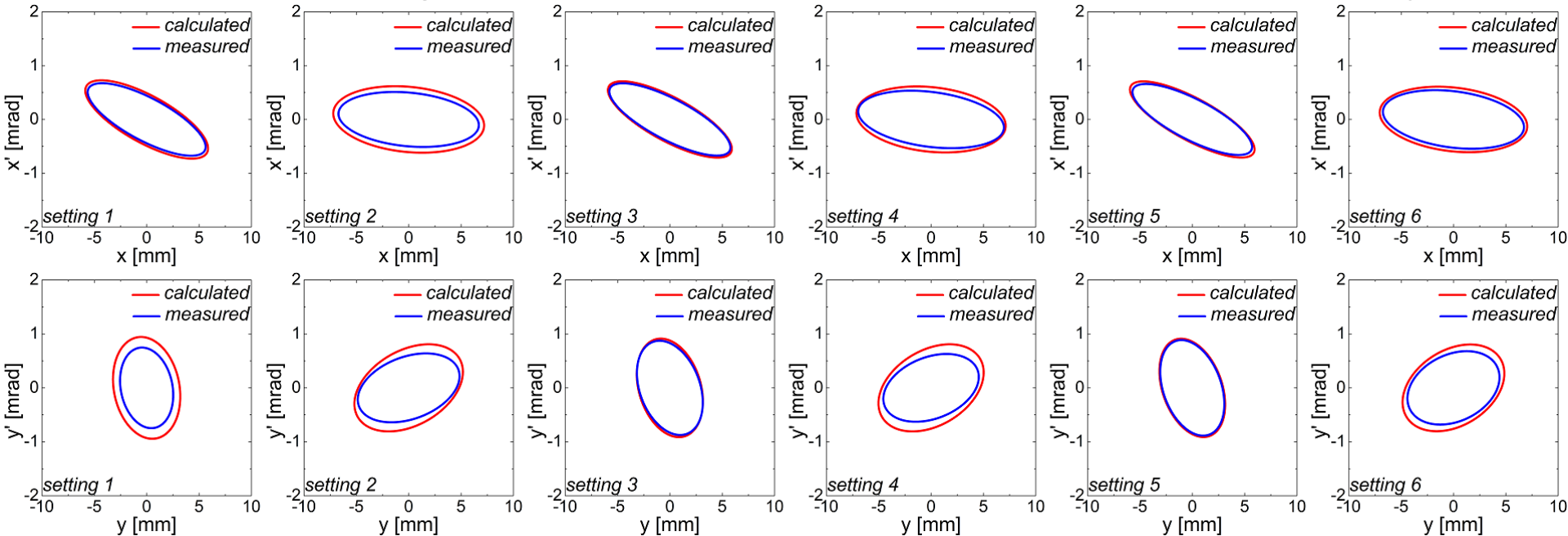
A method has been developed to determine the coupling moments. The resulting second-moment beam matrix at the entrance is:

$$C'_0 = \begin{pmatrix} 12.79 & 1.89 & 0.18 & 0.37 \\ 1.89 & 0.62 & 1.69 & 0.29 \\ 0.18 & 1.69 & 32.18 & 3.49 \\ 0.37 & 0.29 & 3.49 & 0.46 \end{pmatrix}$$



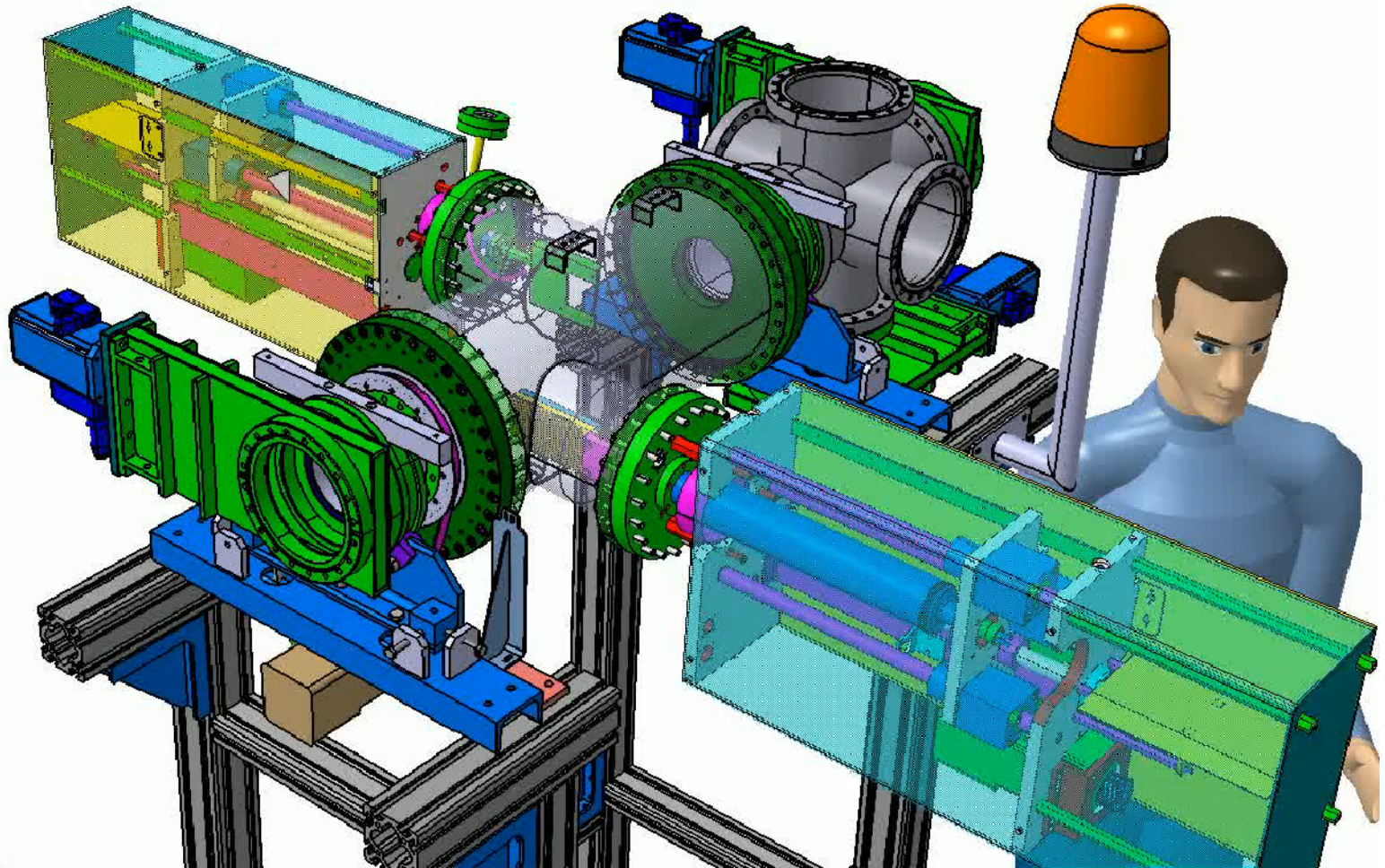
$\epsilon_1 = 2.1$ ,  $\epsilon_2 = 1.2$  mm\*mrad  
coupling parameter  $t = 0.342$

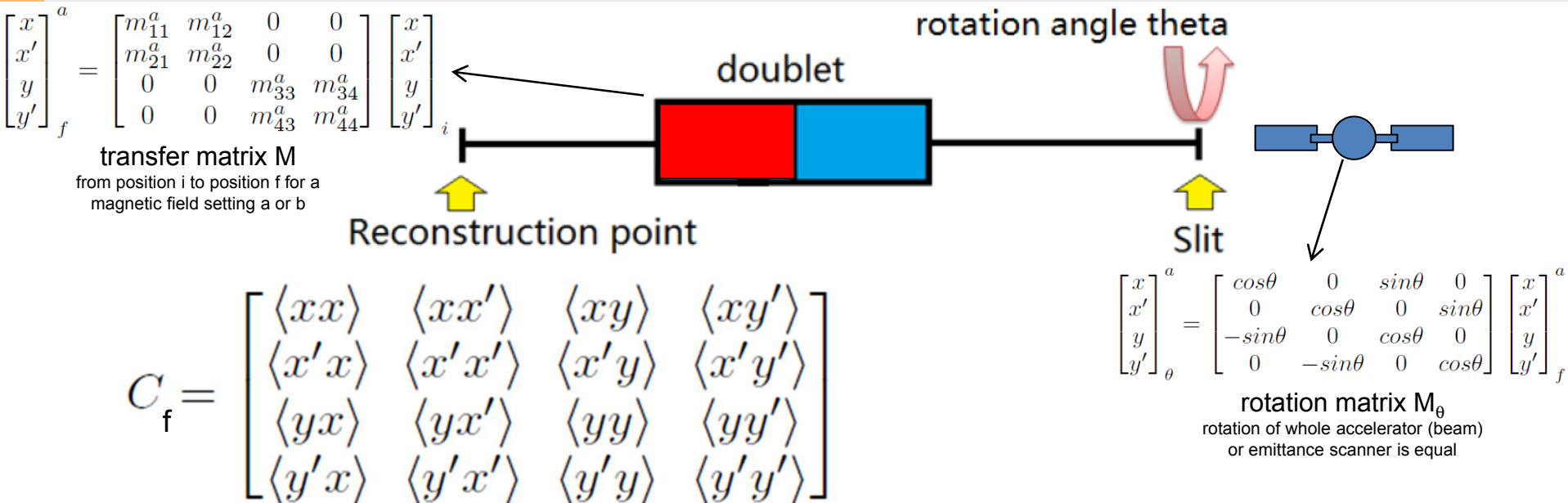
To our knowledge this is the first successful measurement of the 4D-rms-emittance of ions  $\geq 150$  keV/u. In this example removing the correlation would allow for an increase of the beam brilliance by 75%.



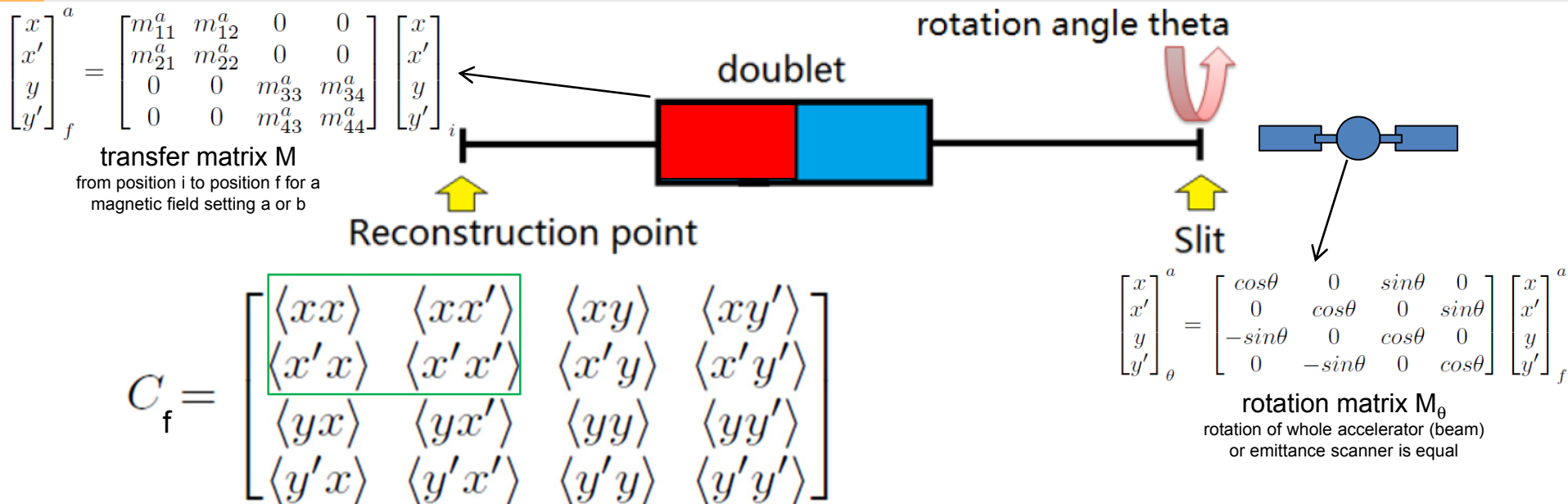
# ROSE

Instead of rotating the beam





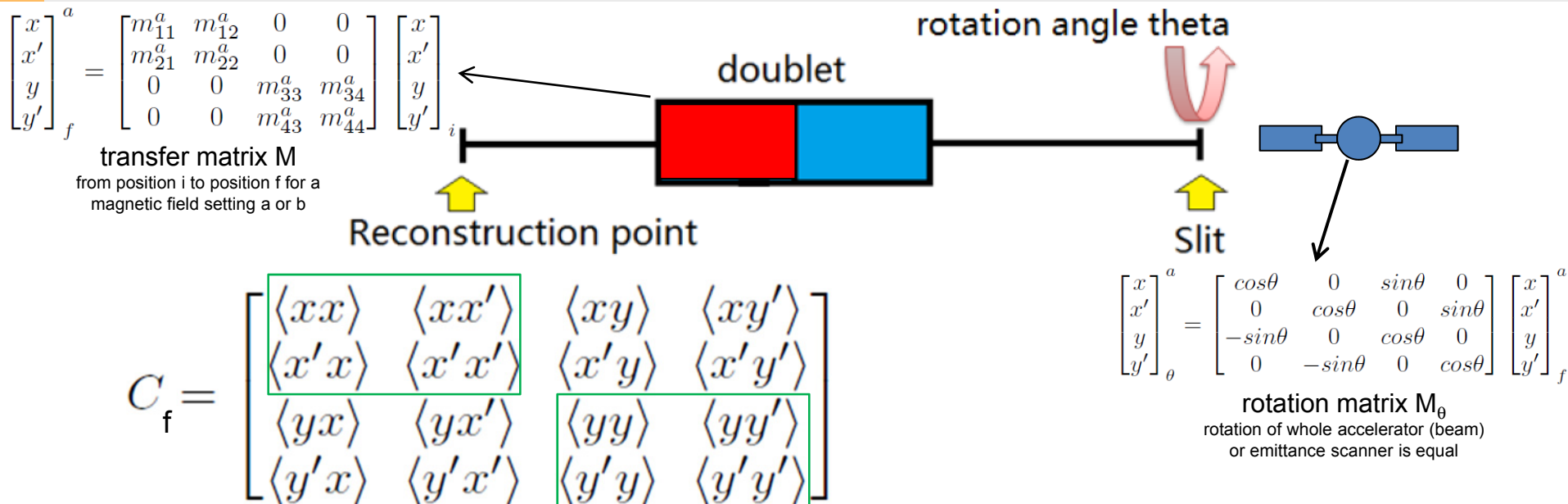
\* Deutsche Patentanmeldung Nr. 102015118017.0 Drehmodul für eine Beschleunigeranlage  
 \*\* Phys. Rev. ST Accel. Beams 16, 044201 (2013).



All values are measured using ROSE at the final position. Knowing the transfer and rotation matrix they can be calculated back to the reconstruction point, the initial position of the original not changing beam matrix  $C_i$ . 100% transmission between initial and final Position is of course required for all settings.

1.  $\theta=0^\circ$  magnet setting a delivers  $\langle xx \rangle_f^a, \langle xx' \rangle_f^a, \langle x'x' \rangle_f^a$

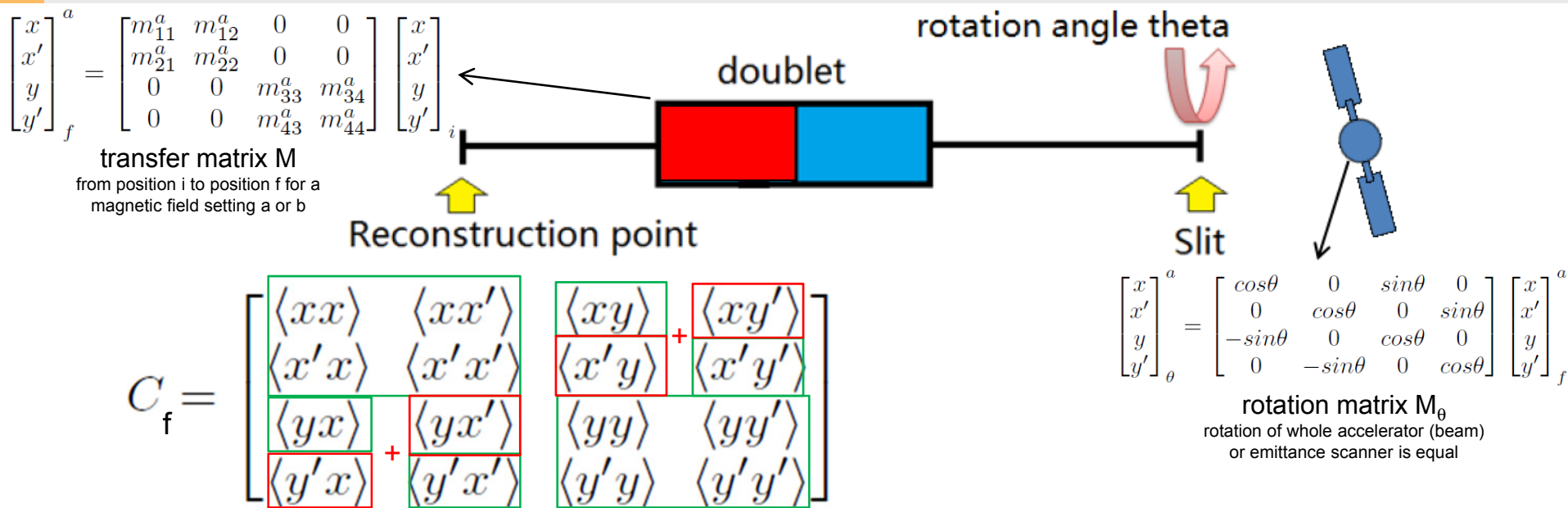
\* Deutsche Patentanmeldung Nr. 102015118017.0 Drehmodul für eine Beschleunigeranlage  
 \*\* Phys. Rev. ST Accel. Beams 16, 044201 (2013).



All values are measured using ROSE at the final position. Knowing the transfer and rotation matrix they can be calculated back to the reconstruction point, the initial position of the original not changing beam matrix  $C_i$ . 100% transmission between initial and final Position is of course required for all settings.

1.  $\theta=0^\circ$  magnet setting a delivers  $\langle xx \rangle_f^a, \langle xx' \rangle_f^a, \langle x'x' \rangle_f^a$
2.  $\theta=90^\circ$  magnet setting a delivers  $\langle yy \rangle_f^a, \langle yy' \rangle_f^a, \langle y'y' \rangle_f^a$

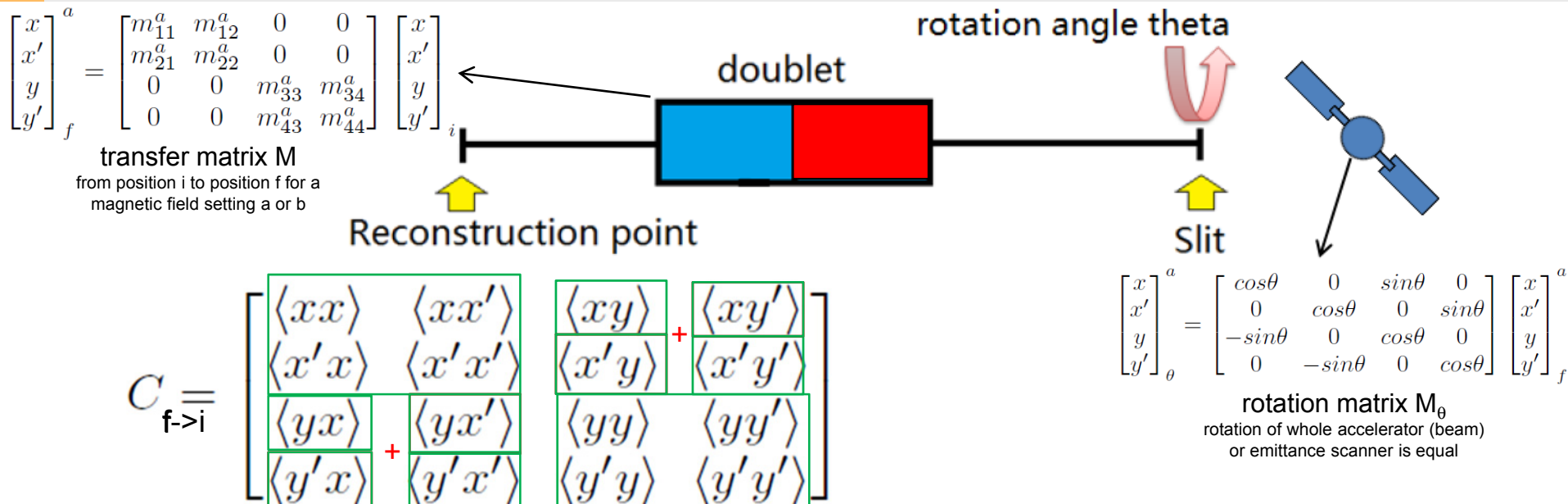
\* Deutsche Patentanmeldung Nr. 102015118017.0 Drehmodul für eine Beschleunigeranlage  
 \*\* Phys. Rev. ST Accel. Beams 16, 044201 (2013).



All values are measured using ROSE at the final position. Knowing the transfer and rotation matrix they can be calculated back to the reconstruction point, the initial position of the original not changing beam matrix  $C_i$ . 100% transmission between initial and final Position is of course required for all settings.

1.  $\theta=0^\circ$  magnet setting a delivers  $\langle xx \rangle_f^a, \langle xx' \rangle_f^a, \langle x'x' \rangle_f^a$
2.  $\theta=90^\circ$  magnet setting a delivers  $\langle yy \rangle_f^a, \langle yy' \rangle_f^a, \langle y'y' \rangle_f^a$
3.  $\theta=45^\circ$  magnet setting a delivers  $\langle yy \rangle_\theta^a, \langle yy' \rangle_\theta^a, \langle y'y' \rangle_\theta^a$

\* Deutsche Patentanmeldung Nr. 102015118017.0 Drehmodul für eine Beschleunigeranlage  
 \*\* Phys. Rev. ST Accel. Beams 16, 044201 (2013).

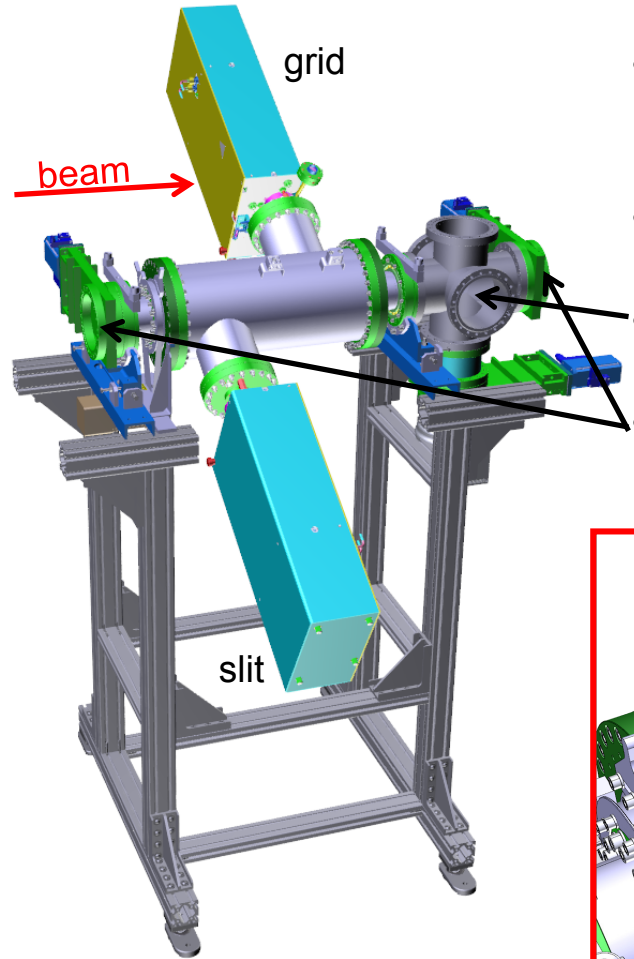


All values are measured using ROSE at the final position. Knowing the transfer and rotation matrix they can be calculated back to the reconstruction point, the initial position of the original not changing beam matrix  $C_i$ . 100% transmission between initial and final Position is of course required for all settings.

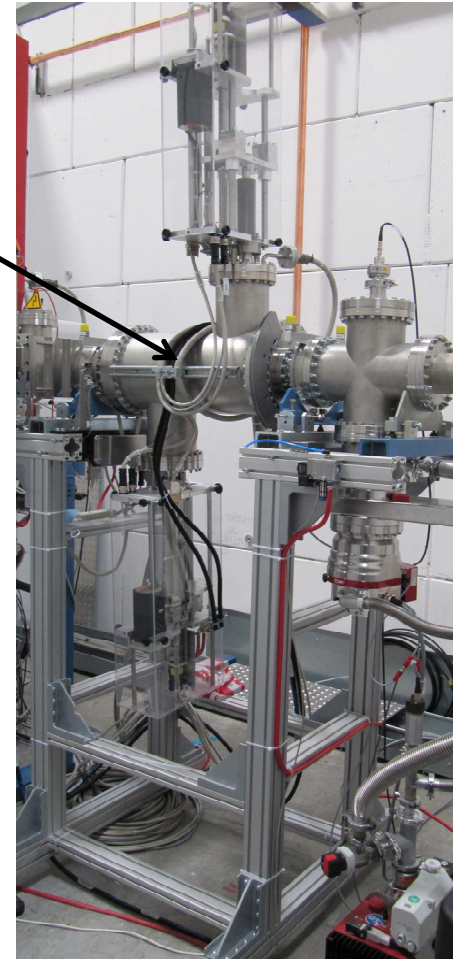
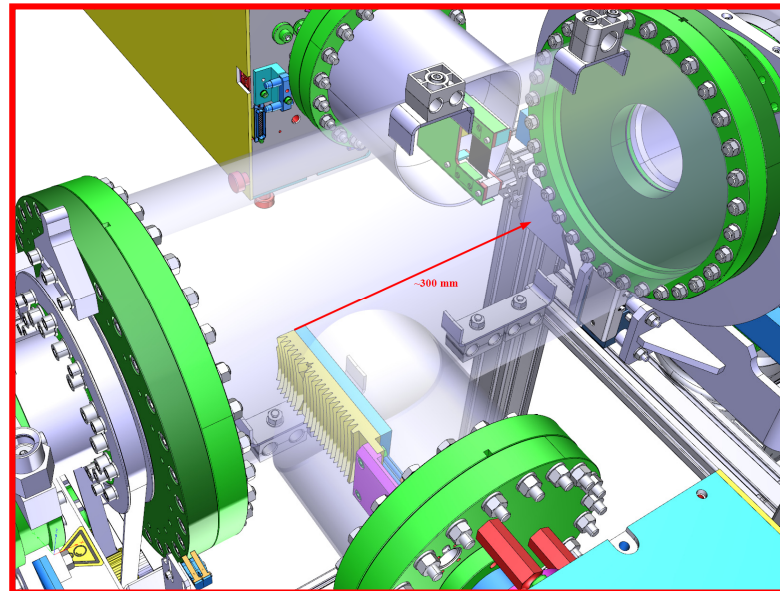
1.  $\theta=0^\circ$  magnet setting **a** delivers  $\langle xx \rangle_f^a, \langle xx' \rangle_f^a, \langle x'x' \rangle_f^a$
2.  $\theta=90^\circ$  magnet setting **a** delivers  $\langle yy \rangle_f^a, \langle yy' \rangle_f^a, \langle y'y' \rangle_f^a$
3.  $\theta=45^\circ$  magnet setting **a** delivers  $\langle yy \rangle_\theta^a, \langle yy' \rangle_\theta^a, \langle y'y' \rangle_\theta^a$
4.  $\theta=45^\circ$  magnet setting **b** delivers  $\langle xx \rangle_\theta^b$

**only 4 measurements are needed to measure the full beam matrix**

\* Deutsche Patentanmeldung Nr. 102015118017.0 Drehmodul für eine Beschleunigeranlage  
 \*\* Phys. Rev. ST Accel. Beams 16, 044201 (2013).



- slit & grid mounted on opposite sides to minimize torque
- cables wrapped around chamber
- fixed pumping chamber
- two gate valves





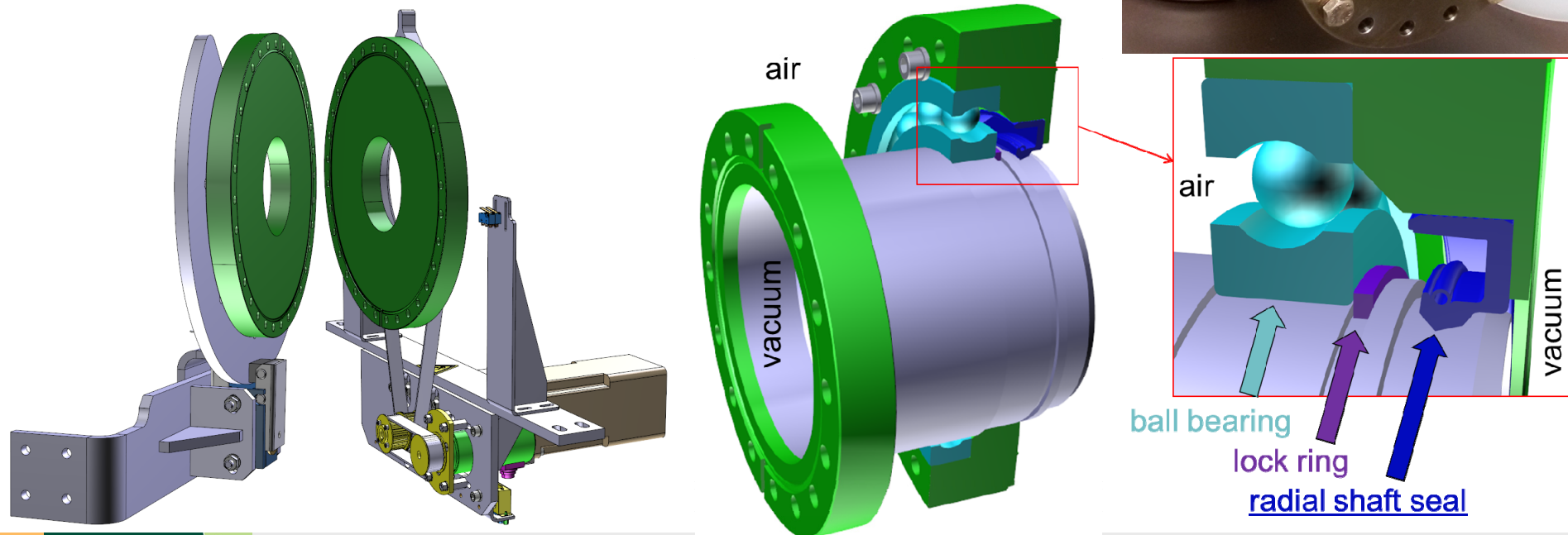
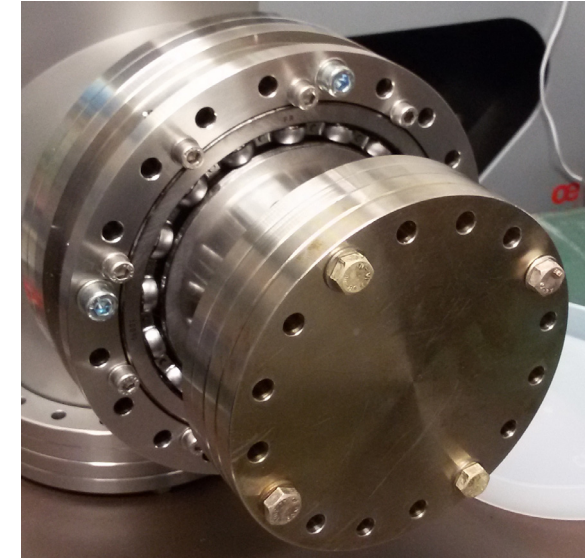
# ROSE

## Technical solutions

- end switches separated by  $180^\circ$
- disk brake (closed during measurements)
- motor driver with belts ( $\delta\theta \leq 0.5^\circ$ )
- $90^\circ$  - rotation slowed actively to  $\approx 30$  sec

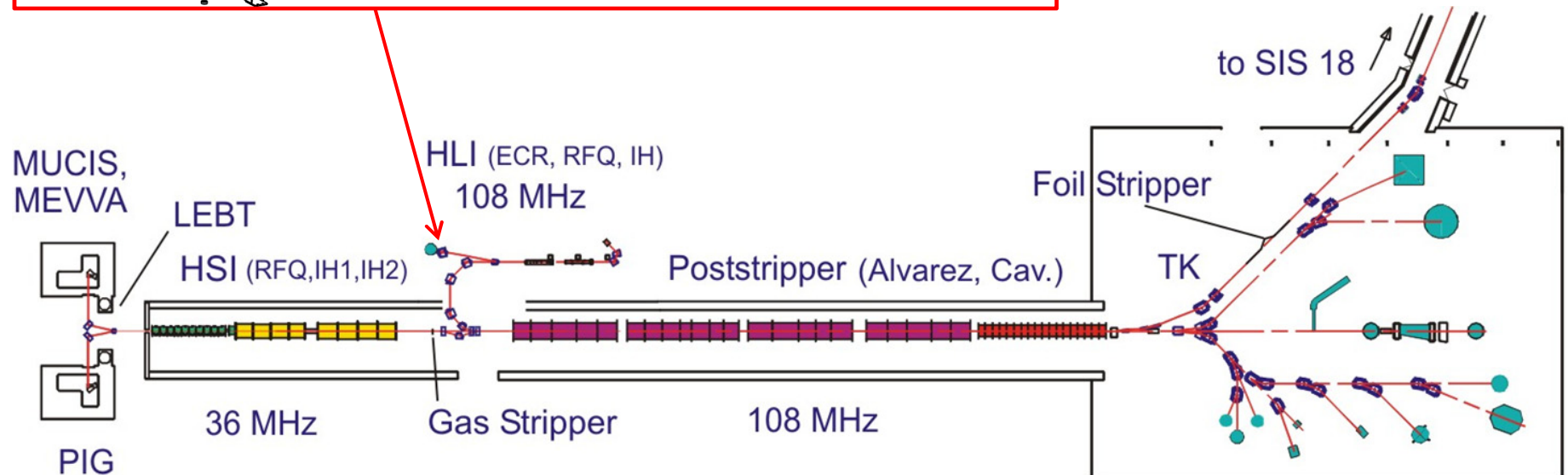
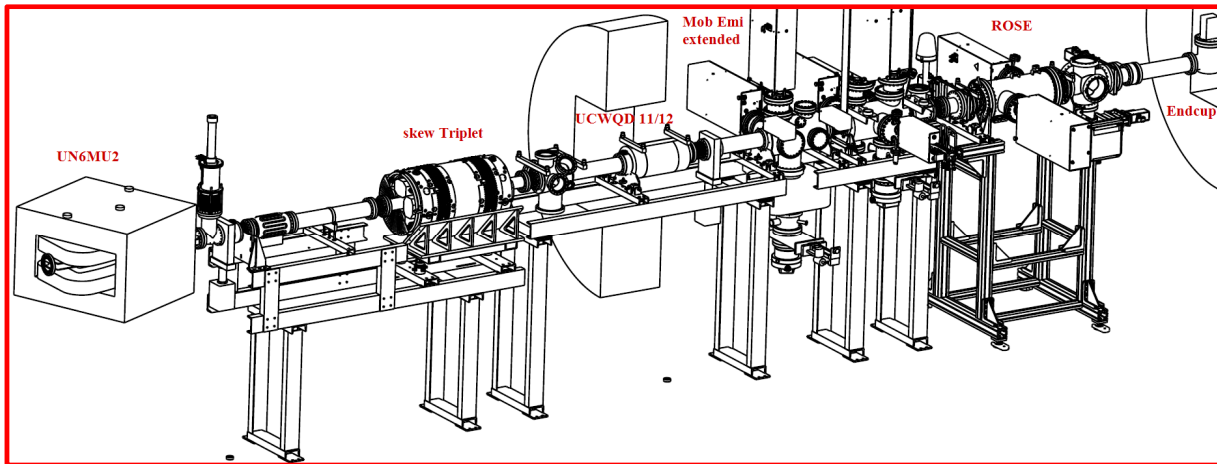
### Vacuum issues:

- static pressure  $\approx 5 \times 10^{-8}$  mbar
- max. pressure during rotation  $\approx 9 \times 10^{-8}$  mbar
- recovery time  $\approx 1$  min



# ROSE commissioning setup

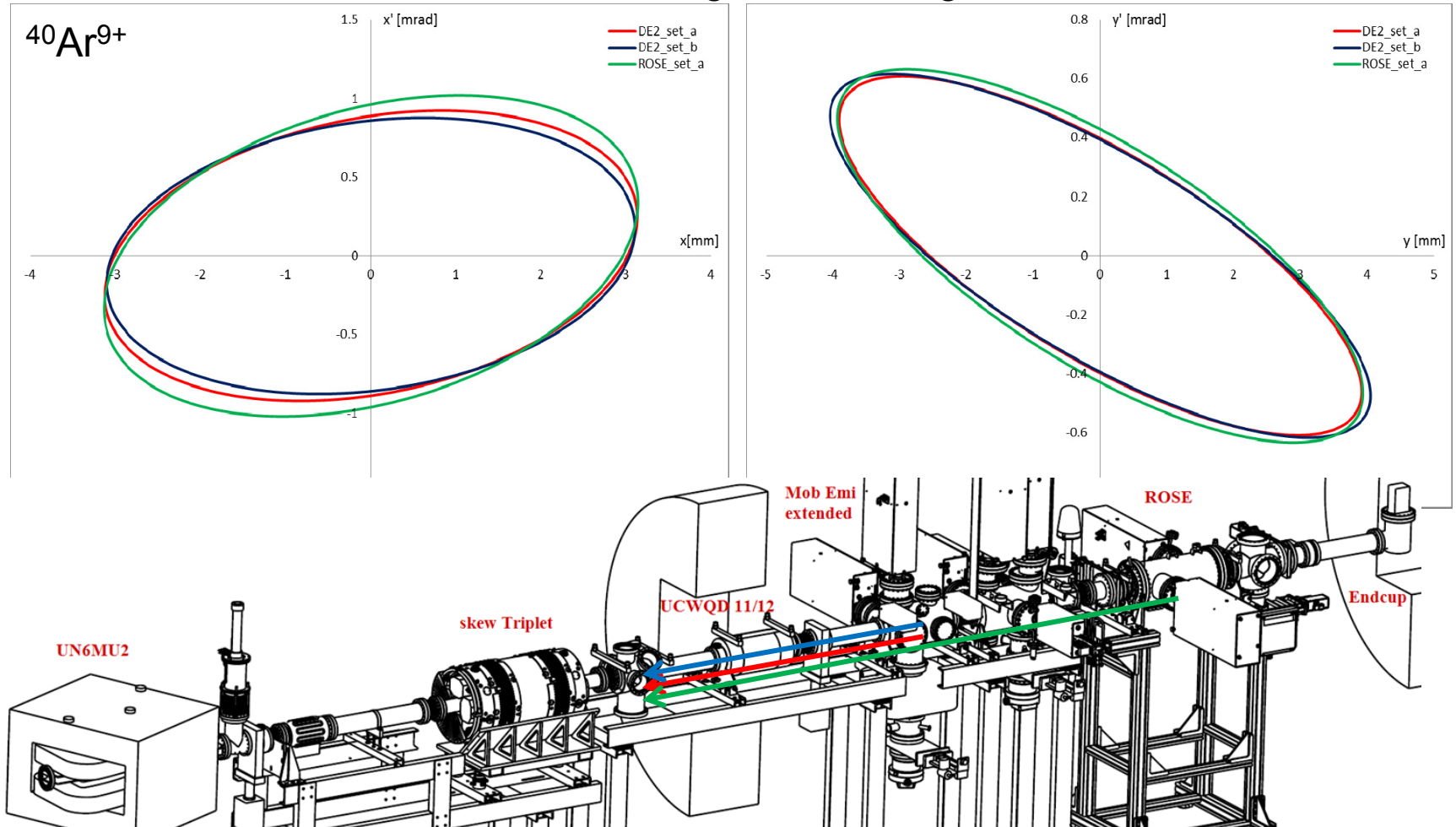
- measurements at exit of GSI's HLI
- 1.4 MeV/u of  $^{40}\text{Ar}^{9+}$  and  $^{83}\text{Kr}^{13+}$
- skew triplet to create  $x \leftrightarrow y$  correlations
- full transmission



# ROSE commissioning

## Benchmarking

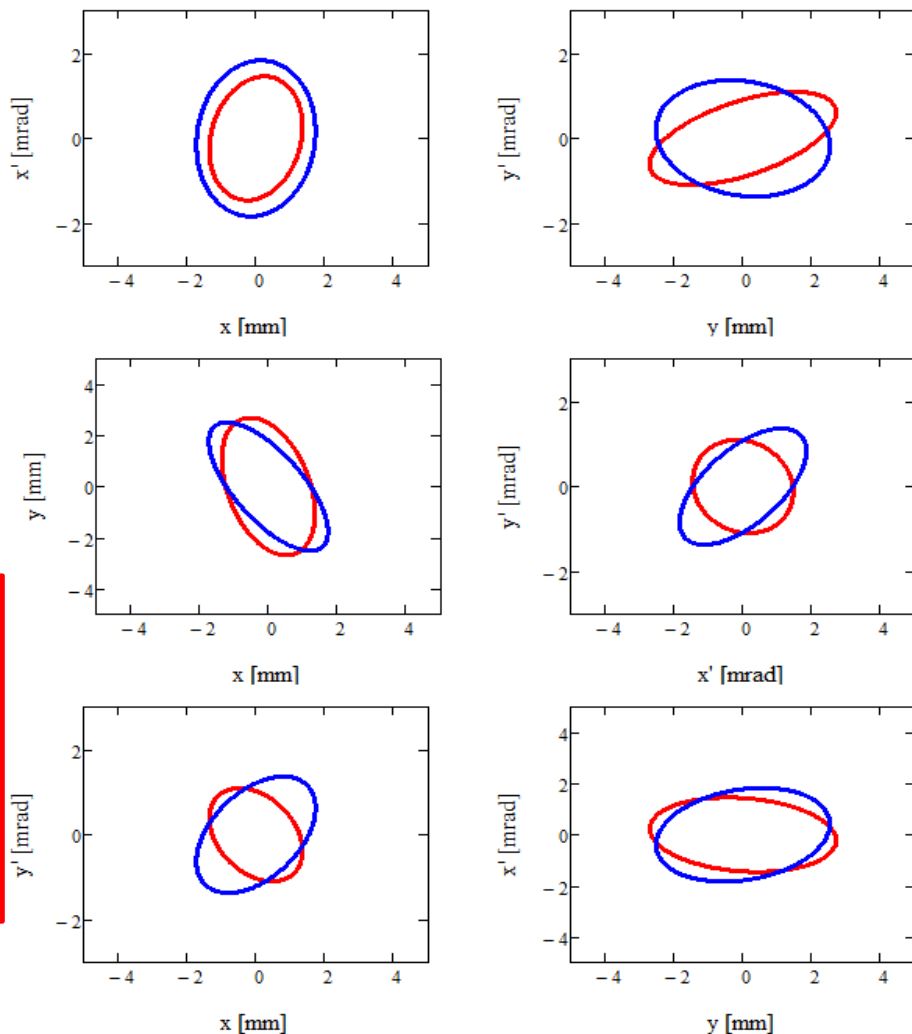
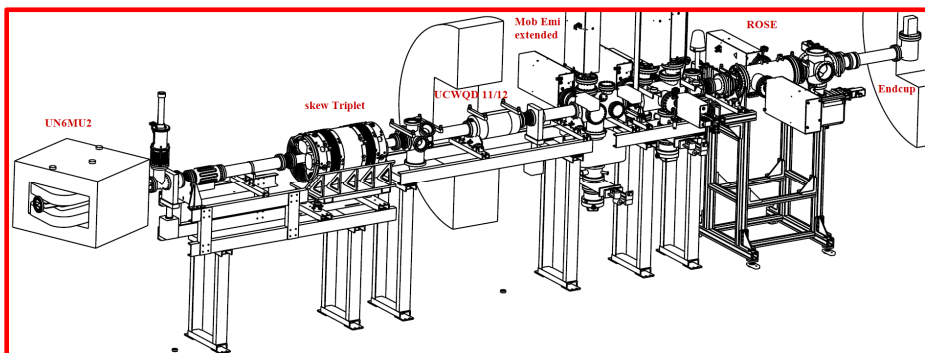
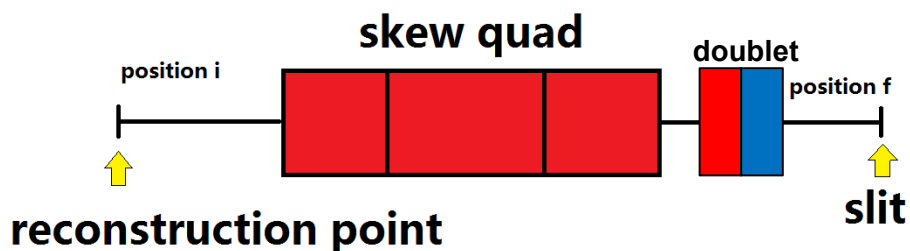
The first commissioning beam time mainly served to commission the hard- and software of ROSE and to benchmark it against existing emittance scanners.



# ROSE commissioning

## 4d emittance measurement of $^{83}\text{Kr}^{13+}$

Slit



red skew off, blue skew on

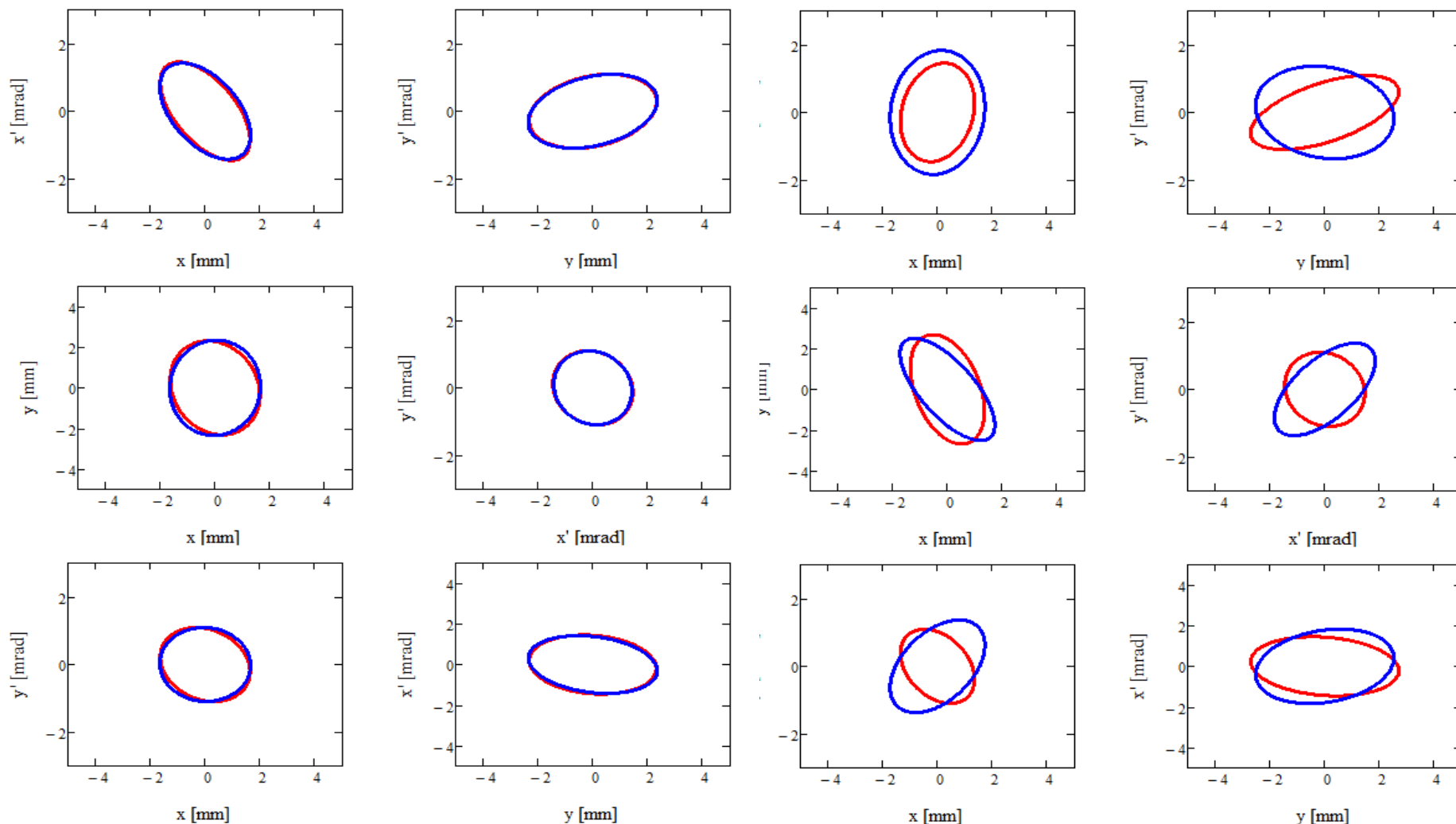
# ROSE commissioning

## 4d emittance measurement of $^{83}\text{Kr}^{13+}$



Reconstruction point in front of skew

Slit



**red skew off, blue skew on**



$\langle RR \rangle$ ,  $\langle PP \rangle$ , and  $\langle PR \rangle$  at  $0^\circ$  for setting "a".

-----  $90^\circ$  -----

-----  $45^\circ$  -----

$45^\circ$  for setting "b"

beam matrix is a function of

$$M_{beam} = f \left( \begin{matrix} \langle RR \rangle_{00}^a, \langle RR \rangle_{00}^b, \langle PR \rangle_{00}^a \\ \langle RR \rangle_{90}^a, \langle RR \rangle_{90}^b, \langle PR \rangle_{90}^a \\ \langle RR \rangle_{45}^a, \langle RR \rangle_{45}^b, \langle PR \rangle_{45}^a \\ \langle RR \rangle_{45}^b, \langle RR \rangle_{45}^b, \langle PR \rangle_{45}^b \end{matrix} \right)$$

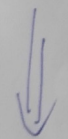
error analysis.

$\langle RR \rangle_{00}^a \rightarrow [\langle RR \rangle + \sigma_1 \langle RR \rangle]_{00}^a = \langle m \rangle_{00}^a \quad \left| \frac{\sigma \langle RR \rangle}{\langle RR \rangle} \right| \approx 10\% \quad \text{distribute like Gaussi}$   
 $\langle PP \rangle_{00}^a \rightarrow [\langle PP \rangle + \sigma_2 \langle PP \rangle]_{00}^a = \langle n \rangle_{00}^a$

-----

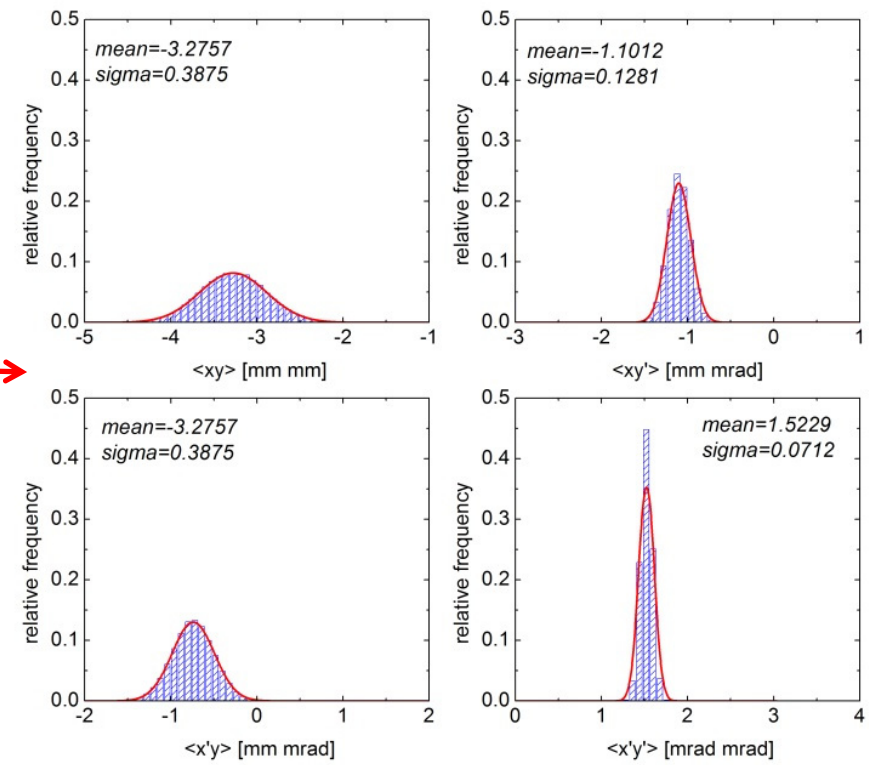
$\langle RR \rangle_{45}^b \rightarrow [\langle RR \rangle + \sigma_{12} \langle RR \rangle]_{45}^b = \langle n' \rangle_{45}^b$

$$M_{beam}(\text{with error}) = f \left[ \begin{matrix} \langle m \rangle_{00}^a, \langle n \rangle_{00}^a, \langle n' \rangle_{45}^b \\ \dots \\ \dots \\ \dots \end{matrix} \right]$$



$\Sigma_1$   
 $\Sigma_2$   
t

# Error studies



Each measured moment entering into the evaluation was varied randomly following a Gaussian distribution centered on its measured value



# Error studies



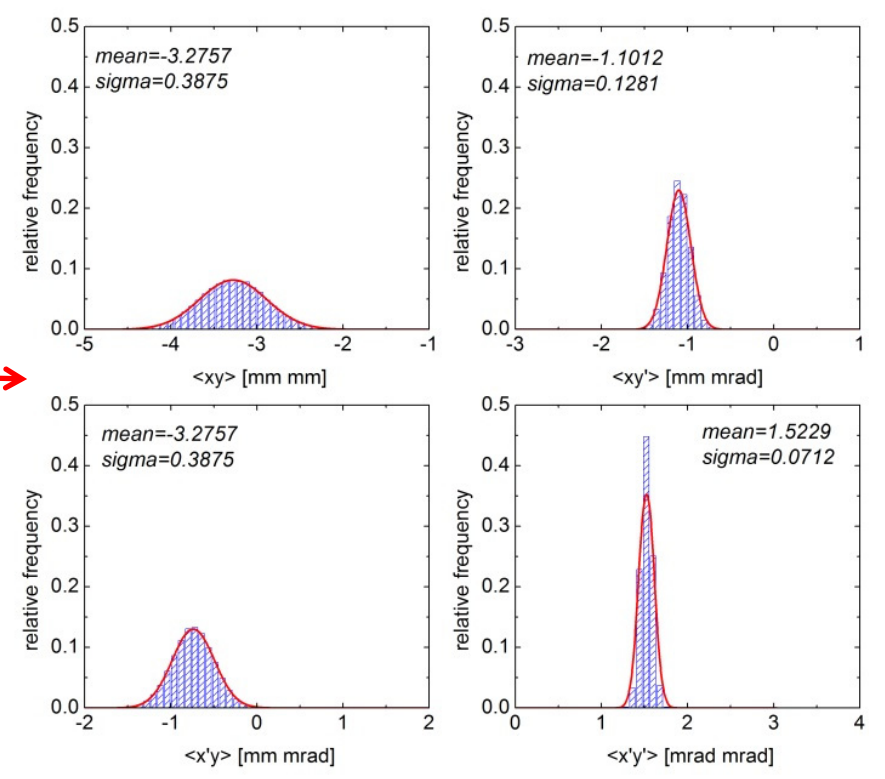
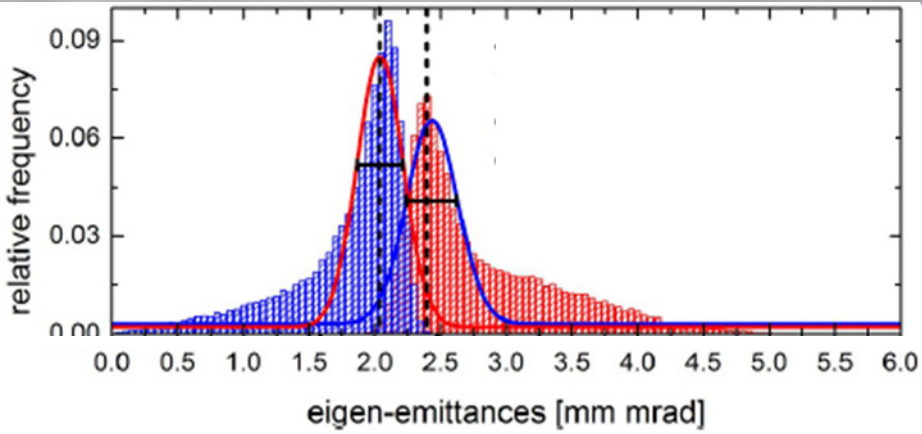
$\langle RR \rangle$ ,  $\langle PP \rangle$ , and  $\langle RP \rangle$  at  $0^\circ$  for setting "a".  
 $90^\circ$   
 $45^\circ$   
 $45^\circ$  for setting "b"

beam matrix is a function of

$$M_{beam} = f \begin{pmatrix} \langle RR \rangle_{0^\circ}^a, \langle RR \rangle_{90^\circ}^a, \langle RR \rangle_{45^\circ}^a \\ \langle PP \rangle_{0^\circ}^a, \langle PP \rangle_{90^\circ}^a, \langle PP \rangle_{45^\circ}^a \\ \langle RP \rangle_{0^\circ}^a, \langle RP \rangle_{90^\circ}^a, \langle RP \rangle_{45^\circ}^a \end{pmatrix}$$

error analysis.

$$\langle RR \rangle_{0^\circ}^a \rightarrow [\langle RR \rangle + \sigma_1 \langle RR \rangle]_{0^\circ}^a = m_{0^\circ}^a \quad \left| \frac{\sigma \langle RR \rangle}{\langle RR \rangle} \right| \approx 10\% \text{ distribute like Gauss}$$

$$\langle PP \rangle_{0^\circ}^a \rightarrow [\langle PP \rangle + \sigma_2 \langle PP \rangle]_{0^\circ}^a = m_{0^\circ}^a$$


Each measured moment entering into the evaluation was varied randomly following a Gaussian distribution centered on its measured value

From the measured moments derived Eigen-emittances of the HLI 1.4 MeV/u  $^{83}\text{Kr}^{13+}$  beam.

# Summary & Outlook

- We have measured the 4d beam parameters of a  $^{238}\text{U}^{28+}$  beam with a kinetic energy of 11.4 MeV/u using the skew technique.
  - We have developed and successfully commissioned ROSE, a prototype 4d emittance scanner that is independent of ion-species, -current and -energy.
- 
- In the future we would like to
    - decouple the  $^{238}\text{U}^{28+}$  beam using the skew triplet confirming it with ROSE
    - repeat EMTEX creating a flat beam accompanied by ROSE
    - build a two chamber system to gain flexibility and to reduce measurement time
    - And for curiosity we could use the skew to rotate the beam followed by a regular Quadrupole triplet to decouple the beam in its new coordinate system!
- 
- With **NTG Neue Technologien GmbH & Co. KG** we have found an industrial partner. Together we are planning to develop a turnkey 4d emittance scanner for the ion accelerator community.





Thank you very much  
for your attention

