# FLAT ELECTRON BUNCH COMPRESSION AT THE ADVANCED SUPERCONDUCTING TEST ACCELERATOR * 

P. Piot ${ }^{1,2}$, C. R. Prokop ${ }^{1}$, B. E. Carlsten ${ }^{3}$, D. Mihalcea ${ }^{1}$, Y.-E Sun ${ }^{4}$<br>${ }^{1}$ Department of Physics, Northern Illinois University DeKalb, IL 60115, USA<br>${ }^{2}$ Fermi National Accelerator Laboratory, Batavia, IL 60510, USA<br>${ }^{3}$ Los Alamos National Laboratory, Los Alamos, NM, 87544 USA<br>${ }^{4}$ Argonne National Laboratory, Argonne, IL 60439, USA

## Abstract

The generation of flat beam using round-to-flat beam conversion of an incoming canonical-angular-momentum dominated electron beam could have important application in the field of advanced acceleration techniques and accelerator-based light source. In this paper we explore the temporal compression of flat beams and especially compare the resulting phase space dilutions with the case of round beam. Finally, we propose and detail a possible experiment to investigate the flat-beam bunch compression at the Advanced Superconducting Test Accelerator currently in construction at Fermilab.

## INTRODUCTION

An important asset of the ASTA photoinjector [1] is its capability to generate beams with high-transverse emittance ratios known as flat beams. Immersing the photocathode in a magnetic field introduces a canonical angular momentum $\langle L\rangle=e B_{0} \sigma_{c}^{2}$, with $B_{0}$ the magnetic field on the photocathode surface, and $\sigma_{c}$ the RMS transverse size of the drive-laser spot on the photocathode [2]. As the beam exits the solenoidal field the angular momentum is purely kinetic resulting in a beam coupled in the two transverse planes. The transverse eigen-emittances (the eigenvalues of the beam matrix) are not degenerated. Three skew quadrupoles in the beamline can apply the torque necessary to cancel the angular momentum [3, 4]. In this process the final beam's transverse emittances, downstream of the round-to-flat-beam (RFTB) converter, equates the eigenemittances [3]

$$
\begin{equation*}
\left(\varepsilon_{x, i}, \varepsilon_{y, i}\right)=\left(2 \beta \gamma \mathcal{L}, \frac{\varepsilon_{u}^{2}}{2 \beta \gamma \mathcal{L}}\right), \tag{1}
\end{equation*}
$$

where $\varepsilon_{u}$ is the normalized uncorrelated emittance of the magnetized beam prior to the transformer, $\beta$ and $\gamma$ the Lorentz factors, $\mathcal{L} \equiv\langle L\rangle / 2 p_{z}$, and $p_{z}$ is the longitudinal momentum. Note that the product $\varepsilon_{x, i} \varepsilon_{y, i}=\left(\varepsilon_{u}\right)^{2}$. In our notations, the smaller emittance is associated to the vertical direction and the emittance ratio $\rho \equiv \varepsilon_{x, i} / \varepsilon_{y, i}>1$. If compressed these flat beams may have applications in Smith-Purcell FELs [5] or for beam-driven acceleration

[^0]techniques using asymmetric structures [6]. It may also be possible to mitigate the bending-plane emittance growth in the bunch compressor [7]. Finally, when combined with transverse-to-longitudinal emittance-exchange techniques, the RFTB method enables repartitioning of the beam emittance within the three degrees of freedom.

## FLAT-BEAM GENERATION

A description of the ASTA photoinjectotr and its performances associated to round beams generation is presented in Ref. [1]; see Fig. 1. The electron source includes of a $1.3-\mathrm{GHz} 1+1 / 2$ radiofrequency (rf) gun [8] surrounded by two solenoids. The generated beam is then injected in two superconducting rf (SRF) cavities and accelerated up to 50 MeV . A set of three skew quadrupoles (RFTB in Fig. 1) located downstream of the accelerating section can be used to transform an angular-momentum-dominated beam into a flat beam. The flat beam can be compressed using a chicane bunch compressor ( BC 1 ) and either send to a user beamline or further accelerated. The longitudinal dispersion of BC 1 is $R_{56}=-0.19 \mathrm{~m}$. A third SCRF cavity (CAV39) operating at 3.9 GHz will eventually be incorporated to correct for nonlinear longitudinal phase space distortions.


Figure 1: Overview of the ASTA photoinjector. The legend is as follows "L1" and "'"L2" are solenoids, "CAV1", "CAV2" and "CAV39" are SRF accelerating cavities, "RFTB" is the round-to-flat beam, "BC1" is a magneticchicane bunch compressor and "ACC1" is the first accelerating cryomodule. The distances (in meters) shown at the bottom are referenced to the cathode surface.

In order to optimize the performance of the flat-beam generation we improve the methods previously introduced [9]. We take the particle coordinates in the transverse trace spaces to be $\widetilde{\mathbf{X}} \equiv\left(x, x^{\prime}\right)$ and $\widetilde{\mathbf{Y}} \equiv\left(y, y^{\prime}\right)$ where $x$ and $x^{\prime}$ are the position and divergence coordinates and $\sim$ is the transpose operator. We introduce the correlation ISBN 978-3-95450-122-9
matrix such that $\mathbf{Y}=C \mathbf{X}$ and statistically extend its definition to $C \equiv\langle\mathbf{Y} \widetilde{\mathbf{X}}\rangle\langle\mathbf{X} \widetilde{\mathbf{X}}\rangle^{-1}$ where $\langle\mathbf{X} \widetilde{\mathbf{X}}\rangle$ and $\langle\mathbf{Y} \widetilde{\mathbf{X}}\rangle$ are $2 \times 2$ blocks of the 4 D beam matrix $\Sigma$. The form of the correlation matrix is constraints and can be shown to be $C_{2,1}=-\left(1+a^{2}\right) / b$ where $a \equiv C_{1,1}=-C_{2,2}$ and $b \equiv C_{1,2}$ which insures $|C|=1$ [9]. Upon knowledge of the incoming $C$ matrix downstream of CAV39, the RFTB is tuned to apply the necessary torque to insure all the elements of $C$ identically vanish downstream of the RFTB [9, 3]. Considering the RFTB configuration implemented at ASTA (three skew quadrupole with 0.167 m effective length separated by 0.38 m ) and limited strengths (typically $k_{1} \leq 30 \mathrm{~m}^{-2}$ ), flat beam generation is only possible for a limited values of the parameters $a$ and $b$ associated to the incoming correlation matrix; see Fig. 2.


Figure 2: Required strength for the 3 skew quadrupoles used in the RFTB [quadrupoles $1,2,3$ are respectively shown in plots (a), (b) and (c) or (d), (e), and (f)]. The right and left columns respectively corresponds to the two possible solutions for the quadrupole settings [10].

The optimization of the flat beam production consists in first optimizing the photoinjector settings (solenoid field, photocathode laser spot size) such to minimmize the 4D emittance $\varepsilon_{4 D} \equiv|\Sigma|^{1 / 4}$ downstream of the accelerating section. The simulation were performed with ASTRA [11] and a multi-objective optimizer [12]. Beside minimizing the 4D emittance a second objective was to maximize the emittance ratio computed as the ratio of the achieved eigen emittances. Figure 3 displays the evolution of the 4D emittance and emittance ratio for an optimized case with parameter listed in Table 1. We confirmed that the 4D emittance after optimization of the flat beam configuration attained a value similar to the round-beam configuration simulated in Ref. [1]; see Table 1.

## FLAT-BEAM COMPRESSION

Downstream of the RFTB, the bunch can be shortened in the BC 1 compressor. Introducing the longitudiISBN 978-3-95450-122-9

Table 1: Comparison of Achieved Beam Parameter for the Round- and Flat-Beam Configuration.

| Parameter | Flat-Beam <br> Configuration | Round-Beam <br> Configuration | Units |
| :---: | :---: | :---: | :---: |
| $Q$ | 3.2 | 3.2 | nC |
| $E$ | 47.18 | 48.77 | MeV |
| $\varepsilon_{x}$ | 105.04 | 5.43 | $\mu \mathrm{~m}$ |
| $\varepsilon_{y}$ | 0.31 | 5.44 | $\mu \mathrm{~m}$ |
| $\varepsilon_{4 D}$ | 5.53 | 5.44 | $\mu \mathrm{~m}$ |
| $\rho$ | $\simeq 334$ | $\simeq 1$ | - |



Figure 3: Evolution of the eigen-emittance (green and blue traces) and associated ratio (red) along the photoinjector. The ordinate $z=8.5 \mathrm{~m}$ corresponds the the exit of CAV39.
nal phase space (LPS) chirp as $\mathcal{C} \equiv-\langle z \delta\rangle /\left\langle z^{2}\right\rangle$ [where $(z, \delta)$ is the longitudinal position and relative momentum offset of the particles], maximum compression occurs at $\mathcal{C}=-1 / R_{56} \simeq 5.2 \mathrm{~m}^{-1}$.

Two major issues arise when compressing a flat beam. Since the RFTB is located between the accelerating section and BC1, the beam dynamics during the flat-beam transformation might be subject to larger fractional momentum spread (as the linac need to impact a correlated energy spread for compression in BC1). Second, the beam dynamics of the flat beam during compression need to be investigated.

In order to explore the behavior of flat beams in the BC 1 compressor as a function of initial emittance ratios $\rho$, we took particle distribution associated to a 3.2 nC bunch and numerically scaled the macroparticle coordinates to produce the desired transverse emittance ratios while constraining the product $\varepsilon_{x, i} \varepsilon_{y, i}=5^{2} \mu \mathrm{~m}^{2}$ to be consistent with the achieved 4D emittance. The simulations are carried with Impact-Z [13] and CsrTrack [14]. The former program simulates CSR using a 1D model (projected model) while the latter program has a more precise but 05 Beam Dynamics and Electromagnetic Fields

CPU-demanding point-to-point (P2P) algorithm. The onedimensional model is valid provided [15]

$$
\begin{equation*}
\mathcal{D}(s) \ll 1, \text { with } \mathcal{D}(s) \equiv \frac{\sigma_{x}(s)}{\sigma_{z}(s)} \sqrt{\frac{\sigma_{x}(s)}{R(s)}} \text {, } \tag{2}
\end{equation*}
$$

where $R(s)$ is the trajectory's radius of curvature and $\sigma_{x}(s)$ and $\sigma_{z}(s)$ are respectively the transverse and longitudinal root-mean-square (RMS) sizes at the curvilinear beamline position $s$.

Due to the large transverse aspect ratio of the bunches, it is anticipated that the projected CSR model used in IMPACTZ is inadequate, thus we use CSRTRACK's P2P model to simulate the flat beams dynamics throughout BC 1 . The parameters used for flat beam simulations follow those used in the previous section, with the exception of the macroparticle horizontal size use in the CsRTRACK P2P model. Due to the much greater transverse dimension we set the horizontal size of the Gaussian macroparticles used in the P2P algorithm to $\sigma_{h}=0.2 \mathrm{~mm}$. In addition, ImPACT-Z simulations were also carried to evaluate the emittance growth in the vertical plan. The simulated emittance growth is shown in Fig. 4 for a 3.2-nC bunch with an initial LPS chirp of $\mathcal{C}=5.2 \mathrm{~m}^{-1}$. As expected the rel-


Figure 4: Bending plane transverse-horizontal emittance growth in BC 1 (red traces) simulated with CsrTrack (dashed line) and Impact-Z (solid lines) as functions of the initial transverse emittance ratio. Corresponding ImPACT-Z results for the vertical emittance (black line), and 4D emittance (magenta).
ative emittance dilution is reduced as the initial emittance ratio $\rho$ increases. The agreement between CsrTrack and IMPACT-Z for the bending-plane emittance dilution is remarkable (within $\sim 30 \%$ ) given the large transverse horizontal beam sizes. In addition, ImPACT-Z predicts that the
vertical emittance increases by a factor 1.5 to 1.8 over the range of considered initial emittance ratios $\rho \in[1,500]$. We also observe that the 4D emittance growth is mitigated for the larger initial flat-beam emittance ratios [7].

## REFERENCES

[1] P. Piot et al., Proc. IPAC10, 4316 (2010).
[2] R. Brinkmann et al., PRSTAB 4 (2001) 053501.
[3] K.-J. Kim, PRSTAB 6 (2003) 104002.
[4] P. Piot et al., PRSTAB 9 (2006) 031001.
[5] C. Prokop et al., APL 96 (2010) 151502.
[6] D. Mihalcea et al., PRSTAB 15 (2012) 081304.
[7] C. Prokop et al., NIMA 719 (2013) 18.
[8] B. Dwersteg et al., NIMA 393 (1997) 93.
[9] E. Thrane et al., Proc. LINAC02, 308 (2002).
[10] Y.-E Sun et al., Proc. LINAC04, 378 (2004).
[11] K. Flöttmann et al., User Manual, DESY (2000).
[12] H. Shang, M. Borland, GeneticOptimizer, private communication (2007).
[13] J. Qiang et al., J. Comp. Phys. 163 (2000) p. 434.
[14] M. D. Dohlus et al., Proc. FEL04. 18 (2004).
[15] Ya. S. Derbenev and V. D. Shiltsev, SLAC-PUB-7181 (1996).


[^0]:    * Work supported the U.S. DoE Contract No. DE-FG02-08ER41532 with NIU and No. DE-AC02-07CH11359 with Fermilab. C.R.P. and B.E.C. are supported by Los Alamos LDRD project \#20110067DR.

