

CHEF: A FRAMEWORK FOR ACCELERATOR OPTICS AND SIMULATION*

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Abstract

We describe CHEF, an application based on an extensive hierarchy of C++ class libraries. The objectives are (1) provide a convenient, effective application to perform standard beam optics calculations and (2) seamlessly support development of both linear and nonlinear simulations, for applications ranging from a simple beamline to an integrated system involving multiple machines. Sample applications are discussed.

INTRODUCTION

Around 1990, one of us (LM) initiated the development of a suite of libraries dedicated to accelerator simulation with an eye on non-linear dynamics [1]. The libraries would take advantage of Automatic Differentiation, a then emerging technique. High order derivatives are the backbone of perturbation analysis in nonlinear dynamics and AD can compute such derivatives to machine precision, something that standard finite difference techniques generally simply cannot deliver.

C++ had just arrived on the scene and was selected as the implementation language because (1) by design, user-defined types can have nearly the same status as native types and (2) it provides comprehensive support for operator overloading. An additional practical consideration was that as, a superset of C, C++ was well-positioned for commercial success and long term viability. This certainly turned out to be a correct assumption.

The vision was to create a framework allowing one to construct applications treating scalar and high order computations on the same footing. In principle, all code describing propagation of a particle through accelerator elements can be made to also implicitly keep track of derivatives with respect to the phase space coordinates through a simple type modification. For example, a `Particle` that would normally hold its phase space state in six doubles needs only to be redeclared as a `JetParticle` holding its state into six `Jet` objects. In this context, a `Jet` is simply a type which, in addition to its state coordinate, also keeps track of derivatives up to some specified order of the map involved in reaching that state.

To some extent, the initial vision was realized. Within a few years, the code base reached a relative level of maturity and the libraries were used in a number of specialized applications. Although correct results were produced, it became increasingly clear that the initial design had serious

flaws. In particular, overhead associated with the utilization of a general n-th order code to perform first order computations (the basis of beam optics) was simply too high. Furthermore, for all the appeal and convenience of overloaded operators, performance was not in line with other available implementations of AD.

In mid-2003, a new development effort was initiated and CHEF was born. The objectives were to build (1) a convenient, intuitive general purpose optics tool supporting multiple popular platforms (2) a modern framework with high level components applicable to design and commissioning problems relevant to next generation machines (ILC, LHC, high intensity proton driver etc.). A decision was made to reuse a substantial portion of our existing code base. However, although the original vision remained as relevant as ever, a major overhaul, with emphasis on efficiency, was imperative. Algorithmic changes were introduced and, in the process, advantage was taken of design idioms and features of C++ not generally available a few years ago. The details belong to another publication; suffice it to say that for first order (optics) computations, performance is now on par with codes based on conventional matrices. For high order computations, performance compares favorably to other available AD libraries. Finally, special attention paid to memory management yielded a substantially reduced dynamic memory footprint.

LIBRARY HIERARCHY

The CHEF framework is based on libraries and components organized in a hierarchical manner as shown in Fig. 1. Note that hierarchical refers to the fact that a library at a given level only depend on the libraries located below it. In this section we provide a brief description of each layer. More details are given in the following sections.

`mxyzptlk`

We can provide here a high level overview of automatic differentiation as implemented by the `mxyzptlk` library. Many interesting details are, unfortunately, beyond the scope of this article. `mxyzptlk` defines the basic types: `Jet_environment`, `Jet`, `Map` and `LieOperator`. `Jet_environment` encapsulates properties of the work environment such as dimensionality of the variable space, the maximum expansion order and the expansion reference point. In general, every `Jet` refers to a specific environment; `Jet` algebra can involve only `Jets` with compatible environments. At this juncture, it should be obvious that `Jet` is the fundamental data type that gen-

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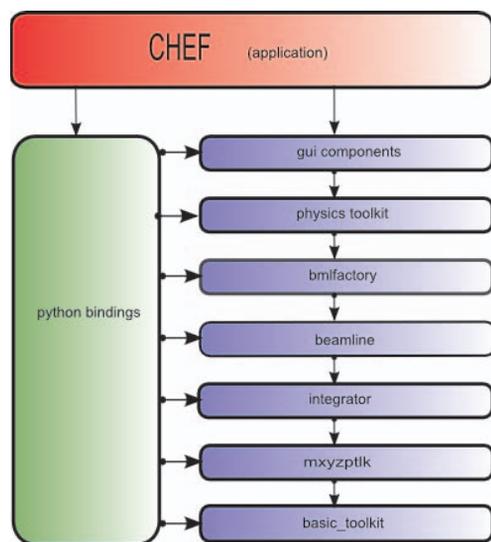


Figure 1: Hierarchical relation between CHEF and underlying libraries.

eralizes a scalar variable. Loosely speaking, it can be interpreted as a representation of a variable augmented by the coefficients of a n th-order differential form. A Map is simply a vector of Jet quantities; each component describes the corresponding coordinate transformation. Through operator overloading, `mxyzptik` provides complete support for all basic operations on Jets as well as trigonometric functions, logarithms, exponential etc. In addition, the composition operator allows Jets and Maps to be concatenated, obviously an essential ingredient of accelerator related computations. The Jet representation in memory is sparse and ordered. Only monomials with non-zero coefficients are stored. They are always ordered by increasing *weight* or total monomial order. The ordering is naturally preserved by the fact that basic add and multiply operations, in terms of which all other operations are ultimately decomposed, are always carried out in an ordered “register” or “scratchpad” that comprises all possible monomials. Elaborate reference counting and memory management strategies are employed to make the computational cost of instantiation and destruction of temporaries as low as possible.

beamline

The beamline library supports a wide variety of standard accelerator components types i.e. `s bend`, `rbend`, `quadrupole`, etc as well as the `beamline` type which is defined as a recursive to preserve hierarchical relations. Internally, the library uses true canonical coordinates, not optical coordinates. As a consequence, *computation within magnetic elements are performed using the true physical field*.

In contrast to many existing codes, *no implicit assumption is made about the the reference trajectory in individual elements*. The default propagation physics (based on ei-

ther on symplectic thin kicks or exact integration) through any element can be overridden by the user. For example, to speed up tracking, one could request physics based on paraxial approximation in arc quadrupoles and a more exact formulation for low-beta quadrupoles. Elements or beamlines can be arbitrarily misaligned in three dimensional space. Note that no implicit assumption is made about the magnitude of the misalignments. Furthermore, geometric edge focusing effects can be accounted for naturally rather than through the introduction of artificial thin edge focusing elements.

bmlfactory

Beamlines can be instantiated from a description in an almost complete subset of the MAD8 language. Full support is provided for variable expressions. There are very few limitations; the most significant omission is a lack of support for macros. The parser is `lex` and `yacc` based and has been in use for a few years already. Very large and complex MAD8 descriptions are routinely successfully parsed. To accommodate the needs of the ILC project, a next generation parser capable of handling the `xsif` format (basically an extended version of the `mad8` format suitable for both linacs and rings) is currently in development. The new parser will also lift restrictions with macros. Other parsers, including a parser for the MAD9 sequence format adopted by MAD-X exist, but are at this point, are not completely functional.

physics_toolkit

The `physics_toolkit` library provides a collection of standard optics and accelerator computations. Lattice functions can be computed for both periodic and non-periodic lattices. In addition to standard uncoupled lattice functions, three different methods are provided to deal with coupled lattice (1) the classical Edward-Teng functions, (2) lattice functions based on spatial eigenmodes projections or (3) a general beam envelope moment (σ -matrix) distribution. Tools for normal form analysis are also available.

python-bindings

A substantial fraction of the libraries public interface is available through `python`, a standard scripting language. The `boost.python` library is used to automatically generate binding code from a specification written in a simple declarative style. reminiscent of IDL.

Of all the popular scripting languages available, `python` provides one of the best “impedance match” to C++, that is, object-oriented features such as operator overloading, inheritance relations and virtual functions have a direct equivalent in `python`. A wide variety of existing `python` wrappers for linear algebra (e.g. LAPACK), signal processing, image processing, networking etc, can be leveraged, resulting in a very powerful facility that can be used to

Element Name	Element Type	Element Length	Initial Position [m]	Initial Angle [mrad]	Initial Energy [MeV]	Initial Energy Spread [MeV]			
ME0	corrector	0	0	0	0	0	0	0	0
DRIFT01	drift	30.4116	26.6116	31.782	33.0274	3	1.0402	-0.009372	-0.009372
DRIFT02	drift	0.184823	26.5966	32.9176	33.0006	3	1.0307	-0.009362	-0.009362
DRIFT03	drift	0.22488	29.1214	32.9008	31.8987	2	3.9472	-0.06111	-0.06111
DRIFT04	drift	0.184823	29.3063	31.9913	32.8841	2	3.9458	-0.057034	-0.057034
DRIFT05	drift	0.301425	29.609	29.8976	34.9742	2	3.9979	-0.05986	-0.05986
DRIFT06	drift	1.11386	30.7216	29.9562	32.8234	2	2.7064	-0.115562	-0.115562
DRIFT07	drift	0.21716	29.5075	30.3058	32.9724	2	2.7064	-0.115562	-0.115562
DRIFT08	drift	0.301425	29.8102	30.3646	34.8809	2	3.9984	-0.118484	-0.118484
DRIFT09	drift	1.11386	30.9262	30.4232	33.1952	2	2.5283	-0.134919	-0.134919
DRIFT10	drift	0.423625	32.4798	31.1719	36.0176	2	4.0758	-0.125911	-0.125911
DRIFT11	drift	0.265655	32.7455	33.3881	38.3466	2	4.1736	-0.127491	-0.127491
DRIFT12	drift	0.274655	33.0181	33.3881	38.3466	2	4.1736	-0.127491	-0.127491
DRIFT13	drift	0.309225	33.3405	34.54	39.399	2	3.9894	-0.128672	-0.128672
DRIFT14	drift	2.10165	35.4465	42.455	39.7724	2	2.737	-0.146613	-0.146613
DRIFT15	drift	0.227381	35.269	40.315	38.6362	2	4.0483	-0.146613	-0.146613
DRIFT16	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT17	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT18	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT19	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT20	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT21	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT22	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT23	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT24	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT25	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT26	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT27	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT28	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT29	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT30	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT31	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT32	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT33	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT34	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT35	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT36	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT37	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT38	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT39	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT40	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT41	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT42	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT43	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT44	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT45	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT46	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT47	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT48	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT49	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555
DRIFT50	drift	0.192877	35.0517	40.3964	38.5773	2	4.0159	-0.146555	-0.146555

Figure 4: The optical functions presented in tabular form.

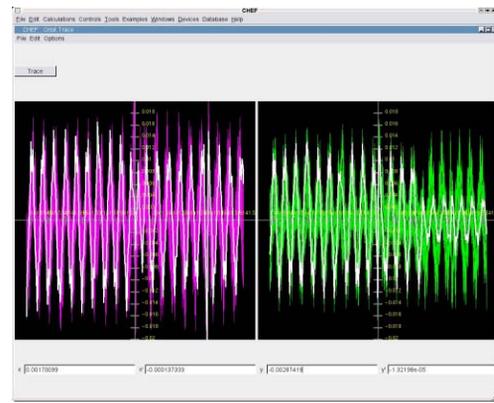


Figure 6: The trajectory tracer.

PHASE SPACE TRACKER

The phase space tracker (Fig. 5) allows one to interactively display phase space Poincaré sections. Such a display can be used to visualize the structure of resonances in a region of interest. Initial conditions of a particle can be specified either explicitly or interactively. Phase space coordinates are displayed as a persistent color-coded point each time the particle returns within the Poincaré section plane. Specifying a new initial conditions changes the point color. Nominally, the tracker provides two two-dimensional phase space cross-section displays. However, because OpenGL is used to render the phase space display window, it is also possible to generate three-dimensional phase space displays e.g. (x, y, p_x) or (x, p_x, p_y) .

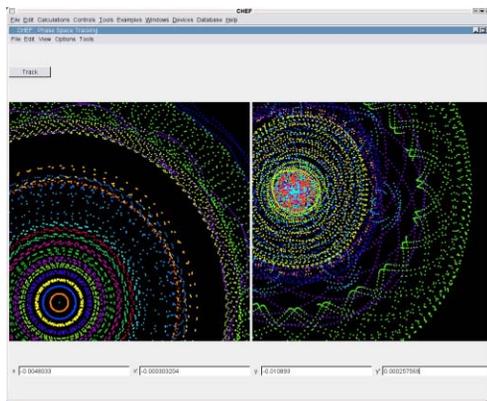


Figure 5: The phase space tracker.

TRACER

The tracer (Fig. 6) allows one to visualize the trajectory(ies) of one or more particles. In the same manner as the phase space tracker, trajectories are rendered persistently using OpenGL (useful for periodic trajectories). The use of OpenGL opens up the interesting possibility (unimplemented at this point) of visualizing beam envelopes and apertures in three-dimensions.

SITE VIEWER

The site viewer (Fig. 7) provides a three-dimensional display of a beamline in space. In addition, it allows one to generate and save floor coordinates for all elements.

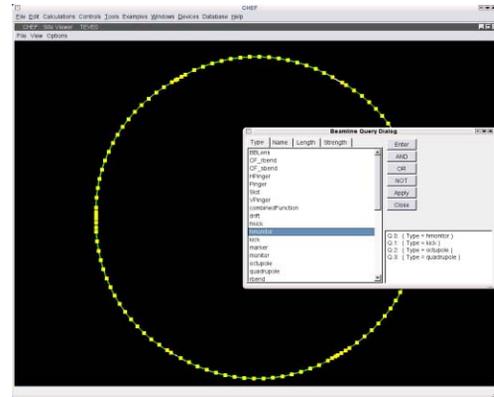


Figure 7: The site viewer. The display show a portion of the Tevatron layout. Horizontal monitors have been highlighted.

CONCLUSION AND FUTURE PLANS

After much effort, CHEF and its underlying libraries have reached a point where they can be put to use and applied to real problems. In particular, the code is being used at Fermilab to study emittance preservation and beam-based alignment in the ILC. Agreement with other codes such as LIAR or Merlin is excellent and we anticipate integrating recently developed linac-specific functionality. Planned future improvements include support for physical apertures (already partially implemented) and particle loss as well as a basic matching capability.

REFERENCES

[1] L. Michelotti, "MXYZPTLK V 3.1 User's guide: A C++ Library for Automatic Differentiation and Differential Algebra. FERMILAB-FN-0535, Jan 1990.