POSSIBLE PHASE LOOP FOR THE GLOBAL DECOUPLING *

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Abstract

The two eigentunes Q_I and Q_{II} , two eigenmode amplitude ratios R_I and R_{II} , and two eignmode phase differences $\Delta \phi_I$ and $\Delta \phi_{II}$, are defined as the coupling observables for the linear weak difference betatron coupling. Simulations were carried out to investigate their behaviors in global decoupling scans. It was found that the amplitude ratios $R_{I,II}$ are more sensitive than the tune split when the decoupling scan is approaching the global uncoupled point, and that the phase differences $\Delta \phi_{I,II}$ tell the right global decoupling direction, the right strength combination of the skew quadrupoles or families. The analytical solution to these six coupling observables is calculated through both the strict matrix approach and the perturbation Hamiltonian approach. The constant phase differences in the right decoupling direction hint a possible global decoupling phase loop. Dedicated beam experiments were carried out at the Relativistic Heavy Ion Collider (RHIC). The preliminary results from the beam experiments are presented. These six parameters can be used for the global decoupling in feedback mode, especially on the non-stop energy ramp.

INTRODUCTION

The global decoupling on the ramp is very important for the Relativistic Heavy Ion Collider (RHIC) polarized proton run, and for the Large Hadron Collider (LHC). The traditional skew quadrupole scan can not be used for the ramp decoupling purpose. The skew quadrupole modulation was put forth at RHIC to fulfill global decoupling on the ramp in feed-forward mode. The coupling angle modulation correction scheme has proven to be fast and robust. It has been applied to accomplish RHIC ramp coupling corrections. However, if considering the changes from ramp to ramp, the global decouling feedback is necessary.

Tune feedback uses the high resolution phase lock loop (PLL) system [1] to track the eigentunes. This system has two limitations that have prevented the implementation of tune feedback during normal RHIC operations. The second results from the effect of coupling on the functioning of the PLL, and on overall system stability when tune feedback is turned on. Measures to deal with these limitations are being taken [2].

During normal operation at RHIC, and more so during the perturbation of skew quadrupole modulation or chromaticity measurement, the PLL tune meter occasionally fails to properly track both eigentunes under some coupling situations. Beyond this, when tune feedback is turned on and the loop is closed to the quadrupole magnets, the feedback system becomes unstable when coupling rotates either of the eigenmodes more than 45 degrees. This poses a big challenge to the robust PLL system to be used for RHIC and LHC tune feedback on the ramp [3]. For the purpose of improved coupling measurement, during the 2004 RHIC run the PLL was re-configured to measure the projections of both eigenmodes in both planes. In addition, a formalism [4] was developed to properly parameterize this measurement.

In this paper we present the six coupling observables defined in that formalism, namely two eigentunes, two eigenmode amplitude ratios, and two eigenmode phase differences. It was found that the amplitude ratios are more sensitive to coupling than the tune split when the machine is working close to the coupling resonance line, and the phase differences tell the right global decoupling direction. If these six parameters can be continuously measured on the ramp, the coupling feedback mode can be applied. Therefore, the robust PLL system is assured on the ramp. For this purpose, during the 2005 RHIC run the PLL was reconfigured to measure the projections of both eigenmodes in both planes.

SIX COUPLING OBSERVABLES

The single particle's motion is presented as [4]

$$\begin{cases} x_n = A_{I,x} \cos[2\pi Q_1(n-1) + \phi_{I,x}] + \\ A_{II,x} \cos[2\pi Q_2(n-1) + \phi_{II,x}] \\ y_n = A_{I,y} \cos[2\pi Q_1(n-1) + \phi_{I,y}] + \\ A_{II,y} \cos[2\pi Q_2(n-1) + \phi_{II,y}] \end{cases}, \quad (1)$$

where Q_I and Q_{II} are the eigentunes. $A_{i,z}$, i = I, II, z = x, y, is the amplitude of the eigenmode *i*'s projection onto the *z* plane. They are non-negative. $\phi_{i,z}$ is the initial phase of the eigenmode *i*'s projection onto the the *z* plane.

Besides the two eigentunes Q_I and Q_{II} , we define another four observables as the weak difference coupling observables. R_I and R_{II} are the eigenmode amplitude ratios,

$$\begin{cases}
R_I = \frac{A_{I,y}}{A_{I,x}} \\
R_{II} = \frac{A_{II,x}}{A_{II,y}}
\end{cases}$$
(2)

 $\Delta \phi_I$ and $\Delta \phi_{II}$ are the eigenmode phase differences,

$$\begin{cases} \Delta \phi_I = \phi_{I,y} - \phi_{I,x} \\ \Delta \phi_{II} = \phi_{II,x} - \phi_{II,y} \end{cases}$$
(3)

 $^{^{\}ast}$ Work supported by U.S. DOE under contract No DE-AC02-98CH10886

The fractional eigentune split $|Q_I - Q_{II} - p|$ has been used as the coupling observable in the conventional skew quadrupole scan decoupling, and it is also currently used in the novel skew quadrupole modulation. The shortcoming to use the eigentune split as the coupling observable is that the skew quadrupole settings have to be changed in order to detect the residual coupling. The eigentune split is not suitable for the decoupling in the feedback mode on the ramp.

SIMULATION

Here we carry out the global decoupling scan simulation to investigate the behaviors of the 6 coupling observables defined above [4]. The smooth accelerator model is used. The uncoupled tunes are $Q_{x,0} = 28.22$, $Q_{y,0} = 29.23$, and the ring circumference is 3813 m. Three skew quadrupoles are equidistantly inserted in the ring. Here we give a 2-D decoupling scan example. Before the 2-D scan, the first skew quadrupole's strength is set to $(k_s dl)_1 = 0.005 \text{ m}^{-1}$. The other two skew quadrupoles are scanned to compensate the global coupling introduced by the first skew quadrupole. From the optics model, the correction strengths for the second and the third skew quadrupoles should be $(k_s dl)_{2,3} = 0.005 \text{m}^{-1}$.

Fig. 1 shows the amplitude ratios $R_{I,II}$ during the 2-D scan. Fig. 2 show the phase difference $\Delta \phi_I$. From the above 2-D decoupling scan, the amplitude ratios are more sensitive than the tune split when the accelerator is working close to the globally uncoupled point. However, their values at one scan point do not tell how to achieve the smaller amplitude ratios. They can be used to check the right or wrong skew quadrupole scan direction.

From Fig. 2, the phase difference $\Delta \phi_I$ and $\Delta \phi_{II}$ keep constant if the decoupling scan is in the right direction. The scan direction is determined by the skew quadrupole strength combination ratio. Therefore, if knowing the relation between the scan direction and the phase differences, from the phase difference measurement at one point it is possible to determine the right skew quadrupole combination to the global uncoupled point. In the right direction decoupling scan, if a π jump is met, then the global uncoupled point is reached. The amplitude ratios can be helpful for the cross-check during the decoupling scan.

ANALYTICAL SOLUTION

The analytical solutions to six coupling parameters can be obtained through the strict matrix and the perturbation Hamiltonian approaches [4]. Here we give the analytical solutions to these six observables from the perturbation Hamiltonian theory [8, 9, 10].

The coupling coefficient C^- is

$$C^{-} = |C^{-}|e^{i\chi} = \frac{1}{2\pi} \int_{0}^{L} \sqrt{\beta_x \beta_y} k_s e^{i[\Phi_x - \Phi_y - 2\pi\Delta \cdot s/L]} dl$$
(4)



Figure 1: Amplitude ratios $R_{I,II}$ in 2-D decoupling scan.



Figure 2: Phase differences $\Delta \phi_I$ in 2-D decoupling scan.

The eigentunes are

$$\begin{cases} Q_I = Q_{x,0} - \frac{1}{2}\Delta + \frac{1}{2}\sqrt{\Delta^2 + |C^-|^2} \\ Q_{II} = Q_{y,0} + \frac{1}{2}\Delta - \frac{1}{2}\sqrt{\Delta^2 + |C^-|^2} \end{cases} (5)$$

The fractional eigentune split is

$$|Q_I - Q_{II} - p| = \sqrt{\Delta^2 + |C^-|^2}$$
(6)

The amplitude ratios are

$$\begin{cases}
R_I = \sqrt{\frac{\beta_y}{\beta_x}} \cdot \frac{|C^-|}{2\nu + \Delta} \\
R_{II} = \sqrt{\frac{\beta_x}{\beta_y}} \cdot \frac{|C^-|}{2\nu + \Delta}
\end{cases}$$
(7)

The phase differences are

$$\begin{cases} \Delta \phi_I = \chi \\ \Delta \phi_{II} = \pi - \chi \end{cases}$$
(8)

Knowing the measured eigentune split and R_I , R_{II} , the uncoupled tune split Δ and the coupling coefficient amplitude $|C^-|$ can be determined,

$$|C^{-}| = \frac{2\sqrt{R_{I}R_{II}}}{1 + R_{I}R_{II}} |Q_{I} - Q_{II} - p|, \qquad (9)$$

$$\Delta = \frac{1 - R_I R_{II}}{1 + R_I R_{II}} (Q_I - Q_{II} - p).$$
(10)

MEASUREMENT WITH PLL

The PLL system [1] is chosen instead of the beam position monitor (BPM) to measure the six coupling parameters. The combination of good pickup sensitivity and narrow bandwidth permits to continuously track tune with tolerable emittance blowup. In the classical PLL tune tracker implementation, the horizontal plane is configured to track eigenmode I and the vertical tracks eigenmode II. However, there is nothing that prevents tracking the projections of both eigenmodes in both planes.

In the present RHIC PLL, to track the projections of both eigenmodes in both planes requires dedicating all four planes of data acquisition to a single ring, leaving the other ring without a PLL tune measurement system during the duration of the desired studies. In the baseband system presently under development[2], the phasesynchronous demodulation will be accomplished entirely in the digital domain, unlike the present system, which requires independent phase-synchronous mixers.

A variety of measurements have been completed during RHIC beam experiments. A presentation of the data in a form most familiar to the accelerator physicist is easily obtained by using four of the six measured parameters to calculate the coupling coefficient and uncoupled tune split. From these, the unperturbed 'set' tunes can be determined. Data taken during a portion of a RHIC acceleration ramp and evaluated in this manner is shown in Figure 3. This data was taken during the polarized proton run, when a working point favorable to polarization was selected above the half-integer, unlike the working point below the halfinteger that was used in the Copper run and mentioned in the previous simulation section of this paper.

The lower image shows the measured eigentunes Q_I (blue continuous trace) and Q_{II} (green continuous trace), as well as the same eigentunes measured at 2 second intervals by the kicked tune system (purple and grey dots). The upper image shows the coupling coefficient (red) and uncoupled tune split (black), calculated as described above. From these, the fractional portion of the unperturbed 'set' tunes $Q_{x,0}$ (black) and $Q_{y,0}$ (red) are calculated and displayed in the lower image. We see that for the first 40 seconds of the ramp the machine is reasonably well decoupled, and the tune split is due almost entirely to the uncoupled tune split. For the next minute or so the coupling becomes large, at times so large that the tune split is due entirely to the coupling. And for the last 30 seconds of data the machine is again reasonably well decoupled. During the interval in which the coupling is large, the PLL continues to track the correct eigenmodes.

CONCLUSION

A method to continuously measure both projections of both eigenmodes has been developed, as has been a proper formalism to parameterize these measurements. Simulations have been carried out to investigate the behavior of the resulting six parameters during 2-D skew quadrudrupole



Figure 3: Tune and coupling data from ramp 7041

scans. Analytical derivations of these parameters were presented, both via the linear coupling action-angle minimization and via the Hamiltonian perturbation theory. The amplitude ratios were found to be favorably sensitive around the globally uncoupled point. From the eigentune split and the amplitude ratios, the uncoupled tunes and the coupling coefficient can be determined. Data from two RHIC ramps was presented, showing the eigentunes and these uncoupled tunes and coupling coefficients. It was shown that the phase differences tell the decoupling directions, or the coupling coefficient's angle. From the phase difference measurement, one can combine the correction skew quadrupole strengths and scan them to reach the globally uncoupled point. In summary, both a technique and a formalism have been demonstrated for measurement and correction of coupling via non-perturbative observation of all projections of the eigenmodes. Efforts to implement this development in normal operations are underway.

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