STUDIES OF SPACE CHARGE LOSS MECHANISMS ON THE ISIS SYNCHROTRON

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Abstract

The ISIS Facility is the pulsed neutron and muon source based at the Rutherford Appleton Laboratory in the UK. Operation centres on the 50 Hz synchrotron, which accelerates $\sim 3 \times 10^{13}$ protons per pulse from 70 to 800 MeV, providing a mean power of about 0.2 MW. As commissioning of a second harmonic RF system is completed, it is expected that the main loss mechanisms will be related to transverse space charge forces, which are particularly strong during the multi-turn injection and trapping processes. Here, we describe progress in ongoing studies to understand more about what drives loss and thus limits intensity. Results from simulations and application of relevant theory are presented, concentrating on the effects thought most important for the ISIS ring. Progress on work looking at the half integer resonance and image effects in the rectangular vacuum vessels is reported, along with work for experimental studies.

INTRODUCTION

ISIS Operations and Space Charge

The ISIS ring has a mean radius of 26 m and accelerates about 3×10^{13} protons per pulse (ppp) from 70 to 800 MeV in 10 ms. The beam is essentially unbunched during the 150 turn charge-exchange injection process, where beam is painted over the transverse acceptances (~400 π mm mr). Most beam loss (~5%) occurs during "trapping", when the beam is non-adiabatically bunched in the first 0.5 ms of acceleration. A dual harmonic RF system [1] is now operational, reducing this loss by maximising capture and improving the bunching factor. Once the optimisation of this system is complete, it is expected that the peak line density reached during trapping, and the associated transverse space charge, will impose the final limit on intensity.

This work addresses only transverse space charge. The nominal tunes of the ISIS ring are Q_x =4.31, Q_y =3.83; during trapping peak incoherent tune depressions are δQ_{incoh} ~0.4 in both planes. Main effects are expected to be the action of half integer resonances ($2Q_x$ =8, $2Q_y$ =7) and image forces related to orbit errors. In this paper we report results of simulations studying these effects.

HALF INTEGER RESONANCE

The Transverse Space Charge Limit

In a previous paper [2] the main theoretical expectations for transverse space charge on ISIS, based on coherent resonance theory, were summarised. Here, simulations are used to bridge the gap between the idealised theoretical models and more realistic beams, within the 2D approximation.

The actual achievable intensity on a ring like ISIS, and its relation to the idealised incoherent and coherent limit, are of significant interest. Whilst the limitations in the (non self-consistent) incoherent picture have been well publicised [3], the limitations in the coherent approach, *as applied to more realistic beams*, have had limited study. When more realistic considerations are included in the coherent model, e.g. increased aperture requirements to accommodate envelope oscillations, or rms emittance (ε_{rms}) increase, the "coherent advantage" may be reduced. In this work we use 2D PIC (particle in cell) simulations, with nominal ISIS parameters, to see how near the coherent limit we might approach, and to gain some insight into the loss mechanisms.



Figure 1: Coherent envelope frequency, peak incoherent tune shifts, and ε_{rms} vs intensity (from simulations).

The ISIS Model and Simulations

Simulations used the ORBIT code [4] and were also confirmed with a new "in house" code under development at ISIS. To ensure consistent and convergent results, comparisons were made between codes and for a range of key simulation parameters. Conservative choices were made: between $5x10^4$ and $2x10^5$ macro-particles, a 128x128 grid for particle binning and field calculations, and >80 space charge kicks per betatron wavelength.

Simulations used a representative, but approximate and idealised 2D model of the ISIS beam. A 4D waterbag with $\varepsilon_{xrms} \approx \varepsilon_{yrms} \approx 65 \pi$ mm mr was matched appropriately, and tracked around the ring for 100 or 1000 turns. Harmonic driving terms ($2Q_x=8$, $2Q_y=7$) were included in the detailed lattice model to give representative half integer stop band widths ($\delta Q_{sb} \approx 0.02$). The models excluded

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momentum spread. Simulations used the injection energy of 70 MeV and the same nominal (zero intensity) Qvalues. Runs were performed for a range of intensities equivalent to *coasting beams* of 0.5 to 9.0×10^{13} ppp. Key beam parameters were recorded, with most values derived from the standard ORBIT functions (but also evaluated independently by the ISIS code). To assess the importance of mismatch two sets of runs were performed: "small" and "large" mismatch, corresponding to initial ~5% and ~25% oscillations in rms widths respectively.

Overall Results and Matching Effects

Overall results are summarised in Figure 1. This shows coherent envelope tunes, peak incoherent tune depressions and ε_{rms} as a function of intensity. Significant beam growth appears *between* the incoherent and coherent limits. Studies of matching are summarised in Figure 2: these show evolution of ε_{rms} and oscillations of envelope width and angle over 100 turns, for the small and large mismatch at 4, 6 and 8×10^{13} ppp. The effect of mismatch is also indicated by error bars on the ε_{rms} in Figure 1. At low intensity, ε_{rms} is reasonably preserved regardless of match. At medium intensity, there is clearly more growth in the mismatched case, although the increase in ε_{rms} is moderate. At high intensity the envelope resonance dominates, and initial match has a small effect.



Figure 2: Evolution of RMS emittance (top) and RMS envelope (bottom) for *small* (blue) and *large* (red) mismatch. Intensities are 4, 6, 8 $\times 10^{13}$ from left to right (horizontal).



Figure 3: Evolution of Envelopes over 100 turns.

Evolution of envelopes for a range of intensities (large mismatch) are shown in Figure 3. At low intensities, motion is characterised by regular, moderate beating, consistent with a conserved ε_{rms} . As intensity increases, the oscillations become larger, eventually resulting in net growth of envelope and ε_{rms} .

Phase Space Distributions, Emittance Growth

The development of particle phase space distributions is shown in Figures 4, 5 and 6. Only one transverse plane is shown (horizontal), as planes are equivalent. Coordinates are normalised: horizontal axis is displacement x (mm), vertical axis is normalised angle $(\alpha/\beta) x + x'$ (mr), with x' the angle, and α , β the lattice Twiss parameters [4].



Figure 4: Evolution of normalised transverse distribution (horizontal) for *small* mismatch (~5% in rms width). Plots show *turns* 1, 21, 41, 61, 81 from left to right and *intensities* 4, 6, 8 $\times 10^{13}$ ppp from bottom to top.



Figure 5: Evolution of normalised transverse distribution for *large* mismatch (~25% in rms width), otherwise as above.



Figure 6: Evolution of normalised transverse distribution near resonance. As above, but at 9×10^{13} ppp.

In these figures, particles are labelled with the same colour over multiple turns (from left to right), corresponding roughly to their emittance on the first turn. Dark red particles start in the "inner-core", and blue particles in the "outer-core". This gives an indication of where halo particles originated. Comparing Figures 4 and 5 shows that a large mismatch generates more halo. However, at high intensities as envelope resonance is approached, mismatch is a minor effect as the beam rapidly blows up, as shown in Figure 6.

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The above results are all for ≤ 100 turns; Figure 7 shows evolution of ε_{rms} over 1000 turns. Error bars indicate estimated numerical uncertainties.



Figure 7: Evolution of ε_{rms} over 1000 turns as a function of intensity.

Interpretation of Results

Taken at face value, the results suggest that with the magnet errors and mismatch levels expected on ISIS, significant beam growth will occur at $6-8x10^{13}$ ppp for a *coasting* 70 MeV beam. Using simple scaling for bunching factor and energy, this suggests operational limits of around 2.1-2.8x10¹³ and 2.8-3.7x10¹³ ppp for single and dual harmonic RF respectively (optimisation of bunching factor may well increase the latter).

Results indicate that the main emittance growth does not occur at the incoherent limit. In addition, the lack of "inner-core" particles appearing in the halo (Figures 4, 5) at low and medium intensities supports the expectation that incoherent resonance is not the main (initial) loss mechanism: the "outer-core" particles are lost first. Phase space structure indicates parametric particle resonance driven by the envelope oscillations (as the envelope approaches resonance). At lower intensities, ideas of the coherent model seem to describe behaviour well, with the expected regular beating of envelopes and expected tune depressions. At about $7x10^{13}$ ppp behaviour changes markedly: envelopes and ε_{rms} indicate substantial growth. Figure 7 shows this clearly, also indicating that the beam redistributes from the non-stationary waterbag to a new stable distribution within about 200 turns.

Further work is planned to understand these results, associated loss mechanisms and possible code limitations. Although some care has been taken to ensure that results were convergent and consistent, the possibility of nonphysical effects remains (particularly with 1000 turn tracking and halo). Ultimately, only comparison with experiment and other algorithms will confirm the results. It is also possible that the simplified 2D beam model will behave quite differently from the real beam.

IMAGE EFFECTS

Initial Calculations with Images

When the possibility of closed orbit errors (off-axis beams) and the ISIS rectangular vacuum vessels are included, additional "image" driving terms appear [3].

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The code under development at ISIS includes a field solver with boundary conditions appropriate for the ISIS vacuum vessels (which has been benchmarked against CST-Studio® [5]): Figure 8. Figure 9 shows results from some initial tests comparing coherent dipole tune shifts from simulations for the "direct" and "image" field solvers. These show the expected results, with coherent dipole shift only appearing with images. This will allow study of image related losses on ISIS.



Figure 8: Example of space charge field solver: potential of off centre waterbag beam in rectangular vessel.





FUTURE AND RELATED WORK

A key aim of this work is to compare theory and simulation with experimental results from ISIS. Diagnostics and experimental methods are being developed to this end, including new profile monitors [6] and procedures for storage ring mode experiments. Simulations will next look at longitudinal effects. Related studies on ISIS injection are reported in [7].

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